Enhancing Regression Models for Complex Systems using Evolutionary Techniques for Feature Engineering

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Abstract This work proposes an automatic methodology for modeling complex systems. Our methodology is based on the combination of Grammatical Evolution and classical regression to obtain an optimal set of features that take part of a linear and convex model. This technique provides both Feature Engineering and Symbolic Regression in order to infer accurate models with no effort or designer's expertise requirements. As advanced Cloud services are becoming mainstream, the contribution of data centers in the overall power consumption of modern cities is growing dramatically. These facilities consume from 10 to 100 times more power per square foot than typical office buildings. Modeling the power consumption for these infrastructures is crucial to anticipate the effects of aggressive optimization policies, but accurate and fast power modeling is a complex challenge for high-end servers not vet satisfied by analytical approaches. For this case study, our methodology minimizes error in power prediction. This work has been tested using real Cloud applications resulting on an average error in power estimation of 3.98%. Our work improves the possibilities of deriving Cloud energy efficient policies in Cloud data centers

being applicable to other computing environments with similar characteristics.

 $\begin{tabular}{ll} \textbf{Keywords} & Automatic modeling} \cdot Complex & Systems \cdot Grammatical & Evolution \cdot Classical regression \cdot Green data centers \cdot Sustainable & Cloud computing \cdot Power modeling \\ \end{tabular}$

1 Introduction

Analytical models, as closed form solution representations, require specific knowledge about the different contributions and their relationships, becoming hard and time-consuming techniques for describing complex systems. Complex systems comprise a high number of interacting variables, so the association between their components is hard to extract and understand as they have non-linearity characteristics [4]. Also, input parameter limitations are barriers associated to classical modeling for these kind of problems.

Otherwise, classical regressions as least absolute shrinkage and selection operator techniques provide models with linearity, convexity and differentiability attributes, which are highly appreciated for describing systems performance. However, the automatic generation of accurate models for complex systems is a difficult challenge that designers have not yet fulfilled by using analytical approaches.

On the other hand, metaheuristics are higher-level procedures that make few assumptions about the optimization problem, providing adequately good solutions that could be based on fragmentary information [6, 7]. They are particularly useful in solving optimization problems that are noisy, irregular and change over time. In this way, metaheuristics appear as a suitable

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approach to meet optimization problem requirements for complex systems.

Some metaheuristics, as Genetic Programming (GP), perform Feature Engineering (FE) that is a particularly useful technique for selecting an optimal set of features that best describe an optimization problem. Those features consist of measurable properties or explanatory variables of a phenomenon. FE methods select adequate characteristics avoiding the inclusion of irrelevant parameters that reduce problem generalization [32]. Finding relevant features typically helps with prediction; but correlations and combinations of representative variables, also provided by FE, may offer a straightforward view of the problem thus generating better solutions.

Grammatical Evolution (GE) is an evolutionary computation technique based on GP. This technique is particularly useful to solve optimization problems and provides solutions that include non-linear terms offering FE capabilities that remove analytical modeling barriers. One of the main characteristics of GE is that it can be used to perform Symbolic Regression (SR) [29]. Also, designer's expertise is not required to process a high volume of data as GE is an automatic method. However, GE provides a vast space of solutions that may be bounded to achieve algorithm efficiency.

In this work we propose a novel methodology for the automatic inference of accurate models that combines the benefits offered by both classic and evolutionary strategies. Firstly, SR performed by a GE algorithm finds optimal sets of features that best describe the system behavior. Then, a classic regression is used to solve our optimization problem using this set of features providing the model coefficients. Finally, our approach provides an accurate model that is linear, convex and derivative and also uses the optimal set of features. This methodology can be applied to a broad set of optimization problems of complex systems. This paper presents a case study for its application in the area of Cloud power modeling as it is a relevant challenge nowadays.

1.1 Motivation

One of the big challenges in data centers is the power-efficient management of system resources. Data centers consume from 10 to 100 times more power per square foot than typical office buildings [30] even consuming as much electricity as a city [23]. Consequently, a careful management of the power consumption in these infrastructures is required to drive the Green Cloud computing [11].

Cloud computing addresses the problem of costly computing infrastructures by providing dynamic resource provision on a pay-as-you-go basis, and nowadays it is considered as a valid alternative to owned high performance computing (HPC) clusters. There are two main appealing incentives for this emerging paradigm: firstly, the Clouds' utility-based usage model allows clients to pay per use, increasing the user satisfaction; secondly, there is only a relatively low investment required for the remote devices that access the Cloud resources [12].

Besides economic incentives, the Cloud model provides also benefits from the environmental perspective, since the computing resources are managed by Cloud service providers but shared among all users, which increases their overall utilization [5]. This fact is translated into a reduced carbon footprint per executed task, diminishing CO_2 emissions. The Schneider Electric's report on virtualization and Cloud computing efficiency [27] confirms that about 17% of annual savings in energy consumption were achieved by 2011 through virtualization technologies.

However, the proliferation of modern data centers is growing massively due to the current increase of applications offered through the Cloud. A single data center, that houses the computer systems and resources needed to offer these services, has a power consumption comparable to 25000 households [21]. As a consequence, the contribution of data centers in the overall consumption of modern cities is increasing dramatically. Therefore, minimizing the energy consumption of these infrastructures is a major challenge to reduce both environmental and economic impact.

The management of energy-efficient techniques and aggressive optimization policies requires a reliable prediction of the effects caused by the different procedures throughout the data center. Server heterogeneity and diversity of data center configurations difficult to infer general models. Also, power dependency with nontraditional factors (like the static consumption and its dependence on temperature, among others) that affect consumption patterns of these facilities may be devised in order to achieve accurate power models.

These power models facilitate the analysis of several architectures from the perspective of the power consumption, and allow to devise efficient techniques for energy optimization. Data center designers have collided with the lack of accurate power models for the energy-efficient provisioning and the real-time management of the computing facilities. Therefore, a fast and accurate method is required to achieve overall power consumption prediction.

The work proposed in this paper makes substantial contributions in the area of power modeling of Cloud servers taking into account these factors. We envision a powerful method for the automatic identification of fast and accurate power models that target high-end Cloud server architectures. Our methodology considers the main sources of power consumption as well as the architecture-dependent parameters that drive today's most relevant optimization policies.

1.2 Contributions

Our work makes the following contributions:

- We propose a method for the automatic generation of fast and accurate models adapted to the behavior of complex systems.
- Resulting models include combination and correlation of variables due to the FE and SR performed by GE. Therefore, the models incorporate the optimal selection of representative features that best describe system performance.
- Through the combination of GE and classical regression provided by our approach, the inferred models have linearity, convexity and differentiability properties.
- As a case study, different power models have been built and tested for a high-end server architecture running several real applications that can be commonly found in nowadays' Cloud data centers, achieving low error when compared to real measurements.
- Testing for different applications (web search engines, and both memory and CPU-intensive applications) shows an average error of 3.98% in power estimation.

The remainder of this paper is organized as follows: Section 2 gives further information on the related work on this topic. Section 3 provides the background algorithms used for the model optimization. The methodology description is presented in Section 4. In Section 5 we provide a case study where our optimization modeling methodology is applied. Section 6 describes profusely the experimental results. Finally, in Section 7 the main conclusions are drawn.

2 Related Work

A complex system can be described as an interconnected agents system exhibiting a global behavior that results from agents interactions [8]. Nowadays, the number of agents in a system grows in complexity, from data traffic scenarios to multisensor systems, as well as the possible interactions between them. Therefore, infering the global behavior, not imposed by a central controller, is a complex and time-consuming challenge

that requires a deep knowledge of the system performance. Due of these facts, new automatic techniques are required to facilitate the fast generation of models that are suitable for complex systems presenting a large number of variables.

The case study presented in this work exhibits high complexity in terms of number of variables and possible traditional and non-traditional sources of power consumption. This issue demands the following review of the state-of-the-art.

In the last years, there has been a rising interest in developing simple techniques that provide basic power management for servers operating in a Cloud, i.e. turning on and off servers, putting them to sleep or using Dynamic Voltage and Frequency Scaling (DVFS) to adjust servers' power states by reducing clock frequency. Many of these recent research works have focused on reducing power consumption in cluster systems [1], [35], [15], [20].

In general, these techniques take advantage of the fact that application performance can be adjusted to utilize idle time on the processor to save energy [13]. However, their application in Cloud servers is difficult to achieve in practice as the service provider usually over-provisions its power capacity to address worst case scenarios. This often results in either waste of power or severe under-utilization of resources. Thus, it is critical to quantitatively understand the relationship between power consumption, temperature and load at the system level by the development of a power model that helps in optimizing the use of the deployed Cloud services.

Currently the state-of-the-art offers various analytical power models. However, these models are architecture-dependant and do not include the contribution of static power consumption, or the capability of switching the frequency modes (DVFS). The authors develop linear regression models that present the power consumption of a server as a linear function of its CPU usage [22], [28]. Some other models can be found where server power is formulated as a quadratic function of the CPU usage [24], [34]. Still, as opposed to ours, these models do not include the estimation of the static power consumption (which has turned to have a great impact due to the current server technology).

Bohra et al. [9] propose a robust fitting to calculate their model that takes into account the correlation between the total system power consumption and component utilization. Our work follows a similar approach but also incorporates the contribution of the static power consumption, its dependence on temperature, and the effect of applying voltage and frequency scaling techniques.

Interestingly, one key aspect in the management of a data center is still not very well understood: controlling the ambient temperature at which the data center operates. Data centers operate in a broad temperature range from 18°C to 24°C but some can be as cold as 13°C [10,25]. However, due to the lack of accurate power models, the effect of ambient temperature on the power consumption of the servers has not been clearly analyzed, preventing the application of optimization models to save energy. On the contrary, the experimental work presented in this paper has been performed in ambient temperatures ranging from 18°C to 25°C. The range selected follows nowadays' practice of operating at higher temperatures [17] and close to the limits recommended by ASHRAE. Although this practice obtains energy savings in the cooling expense [14], the lack of a detailed power model prevents to apply optimization policies.

In our previous work, we have applied the benefits of Particle Swarm Optimization algorithms (PSO) to identify an analytical model that provides accurate results for power estimation [2]. PSO simplifies the power model by significantly reducing the number of predefined parameters and variables used in the analytical formulation. However, as a parameter identification mechanism, this technique does not provide an optimal search of the features that best describe the system power performance, so additional features could be incorporated.

The work presented in this paper outperforms previous approaches in the area of power modeling for enterprise servers in Cloud facilities in several aspects:

- Our approach consists on an automatic method for the identification of an accurate power model particularized for each target architecture. We propose an extensive power model consistent with current architectures.
- The proposed methodology takes into account the main power consumption sources resulting in a multiparametric model to allow the development of power optimization approaches. Different parameters are combined by Feature engineering assuring that the optimal set of features is considered.
- Optimal features are included in a classical regression resulting in a specific model instance for every target architecture that is linear, convex and derivable. Also the execution of the resulting power model is fast, making it suitable for run-time optimization techniques.

3 Algorithm description

3.1 Grammatical Evolution

As previously stated, we work on FE to obtain mathematical expressions that represent different power consumption contributions. These expressions, or features, are derived from the combination of previously collected experimental parameters (in our case of study, they correspond to processor and memory temperatures, fan speeds, processor and memory utilizations, processor frequencies and voltages). We deal with a kind of SR problem to select the relevant features. SR tries to simultaneously obtain a mathematical expression while including the relevant parameters to reproduce a set of discrete data. Besides, GP has proven to be effective in a number of SR problems [33]. However, GP presents some limitations like bloating of the evolution (excessive growth of memory computer structures), often produced in the phenotype of the individual. During the last years, variants to GP like GE appeared as a simpler optimization process [26]. In our approach, GE allows the generation of a new set of optimized features by applying SR. This feature generation is achieved thanks to the use of grammars that define the rules for obtaining mathematical expressions. More concretely, we will use grammars expressed in Backus Naur Form (BNF) [26].

A BNF specification is a set of derivation rules, expressed in the form:

<symbol>::=<expression>

The rules are composed of sequences of terminals and non-terminals. Symbols that appear at the left are non-terminals while terminals never appear on a left side. In this case we can affirm that <code><symbol></code> is a non-terminal and, although this is not a complete BNF specification, we can affirm also that <code><expression></code> will be also a non-terminal, since those are always enclosed between the pair <code>< ></code>. Therefore, in this case the non-terminal <code><symbol></code> will be replaced (indicated ::=) by an expression. The rest of the grammar must define the different alternatives.

A grammar is represented by the 4-tuple N, T, P, S, being N the non-terminal set, T is the terminal set, P the production rules for the assignment of elements on N and T, and S is a start symbol that should appear in N. The options within a production rule are separated by a " $\|$ " symbol.

Figure 1 represents an example of a grammar in BNF, designed for symbolic regression. The final obtained expression will consist of elements of the set of terminals T. These have been combined with the rules of the grammar, as explained previously. Also, grammars can be adapted to bias the search of the relevant

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N = {EXPR, OP, PREOP, VAR, NUM, DIG}
 = \{+, -, *, /, \sin, \cos, \exp, x, y, z,
     0, 1, 2, 3, 4, 5, (, ), .}
S = \{EXPR\}
 = {I, II, III, IV, V, VI}
    <EXPR> ::= <EXPR><OP><EXPR>
              | <PREOP>(<EXPR>)
             | <VAR>
II < OP>
           ::= + | - | * | /
III <PREOP>::= sin| cos | exp
           ::= x | y | z | <NUM>
ΙV
    <VAR>
    <NUM>
           ::= <DIG>.<DIG> | <DIG>
VI
    <DIG>
           ::= 0 | 1 | 2 | 3 | 4 | 5
```

Fig. 1 Example of a grammar in BNF format designed for symbolic regression

features because there is a finite number of options in each production rule.

Regarding both the structure and the internal operators, GE works exactly like a classic Genetic Algorithm (GA) [3]. GE evolves a population formed by a set of individuals, each one constituted by a chromosome and a fitness value. In SR, the fitness value is usually a regression metric like Root Mean Square Deviation (RMSD), Coefficient of Variation (CV), Mean Squared Error (MSE), etc. In GE, a chromosome is a string of integers. In the optimization process, GA operators named selection, crossover and mutation are iteratively applied to improve the fitness value of each individual. In order to compute the fitness function for every iteration and to extract the mathematical expression given by an individual, a decoding process is applied. We refer the reader to [16] to understand the different GA operators. In the following, we explain through an example the decoding process performed in GE, since it clearly explains how better features are automatically selected. Let us suppose that we have the BNF grammar provided in Figure 1 and the following 7-gene chromosome:

21-64-17-62-38-254-2

According to Figure 1, the start symbol is S={EXPR}, hence the decoded expression will begin with this non-terminal:

Solution = <EXPR>

Now, we use the first gene of the chromosome (also called codon, equal to 21 in the example) in rule I of the grammar. The number of choices in that rule is 3. Hence, a mapping function (the modulus operator) is applied:

21 MOD 3 = 0

and the first option is selected <EXPR><OP><EXPR>. The selected option substitutes the decoded non-terminal.

As a consequence, the current expression is the following:

Solution = <EXPR><OP><EXPR>

The process continues with the next codon, 64, which is used to decode the first non-terminal of the current expression, namely, <EXPR>. Again, the mapping function is applied to rule I:

64 MOD 3 = 1

and the second option <PREOP>(<EXPR>) is selected. So far, the current expression is:

Solution = <PREOPR>(<EXPR>)<OP><EXPR>

The next gene, 17, is now taken for decoding. At this point, the first non-terminal in the current expression is <PREOP>. Therefore, we apply the mapping function to rule III, which also has 3 different choices:

17 MOD 3 = 2

and the third option <code>exp</code> is selected. The resulting expression is

Solution = exp(<EXPR>)<OP><EXPR>

Next codon, 62, decodes <EXPR> with rule I:

62 MOD 3 = 2

Value 2 means to select the third option, <VAR>. The resulting expression is:

Solution = exp(<VAR>)<OP><EXPR>

Codon 38 decodes <VAR> with rule IV:

38 MOD 4 = 2

selecting the third option, non-terminal z:

Solution = exp(z) < OP > < EXPR >

Non-terminal <0P> is decoded with codon 254 and rule II:

254 MOD 4 = 2

This value selects the third option, terminal *:

Solution = exp(z)*<EXPR>

The last codon, decodes <EXPR> with rule I:

2 MOD 3 = 2

Value 2 selects the third option, non-terminal <VAR>. So far, the current expression is:

Solution = exp(z)*<VAR>

At this point, the decoding process has run out of codons. That is, we have not arrived to an expression with terminals in all of its components. In GE, the solution to this problem is to reuse codons starting from the first one. In fact, it is possible to reuse the codons more than once. This technique is known as wrapping and mimics the gene-overlapping phenomenon in many organisms [18]. Thus, applying wrapping to our example, the process goes back to the first gene, 21, which is used to decode <VAR> with rule IV:

21 MOD 4 = 1

This result selects the second option, non-terminal y, giving the final expression of the phenotype:

Solution = exp(z)*y

As can be seen, the process does not only perform parameter identification like in a classic regression method. In conjunction with a well-defined fitness function, the evolutionary algorithm is also computing an optimized set of features as mathematical expressions by combining the set of parameters that best fits the target system. Thus, GE is defining the optimal set of features that will derive into the most accurate power model.

3.2 Least absolute shrinkage and selection operator

Tibshirani proposes the least absolute shrinkage and selection operator algorithm (lasso) [31] that minimizes residual summation of squares according to the summation of the absolute value of the coefficients that are less than constant.

The algorithm combines the favourable features of both subset selection and ridge regression like stability, and offers a linear, convex and derivable solution. *Lasso* provides interpretable models shrinking some of the coefficients and setting others to exactly zero values for generalized regression problems.

For a given non-negative value of λ , the *lasso* algorithm solves the following problem:

$$\min_{\beta_0,\beta} \left(\frac{1}{2N} \sum_{i=1}^{N} (y_i - \beta_0 - x_i^T \beta)^2 + \lambda \sum_{j=1}^{p} |\beta_j| \right)$$
 (1)

where:

- $-\beta$: vector of p components. Lasso algorithm involves the L^1 norm of β
- $-\beta_0$: scalar value.
- -N: number of observations.
- y_i : response at observation i.
- x_i : vector of p values at observation i.

- λ : non-negative regularization parameter corresponding to one value of Lambda. The number of nonzero components of β decreases as λ increases.

At the end, we combine the use of GE that generates the set of relevant features with *lasso* that computes the coefficients and the independent term in the final linear model

As a result, our GE+lasso framework solves our optimization problem that targets the generation of accurate power models for high-end servers.

4 Devised Methodology

The fast and accurate modeling of complex systems is a relevant target nowadays. Modeling techniques allow designers to estimate the effects of variations in the performance of a system. Complex systems present non-linear characteristics as well as a high number of potential variables. Also, the optimal set of features that impacts the system performance is not well known as many mathematical relationships can exist among them.

Hence, we propose a methodology that considers all these factors by combining the benefits of both GE algorithms and classical *lasso* regressions. This technique provides a generic and effective modeling approach that could be applied to numerous problems regarding complex systems, where the number of relevant variables or their interdependence are not known.

Figure 2 shows the proposed methodology approach for the optimization of system modeling problem. Detailed explanations of the different phases are summarized in the following subsections.

4.1 GE feature selection

Given an extensive set of parameters that may cause an effect on system performance, FE selects the optimal set that best describes the system behavior. Also, this technique, which is provided by GE, avoids the inclusion of irrelevant features while incorporating correlations and combinations of representative variables.

The input to our approach consists of a vector of initial data that includes the entire set of variables x_n extracted from the system.

$$\mathbf{y} = g_1(x_1, x_2, x_3, \dots, x_n) \tag{2}$$

All these parameters are entered in the GE algorithm to start the optimization process.

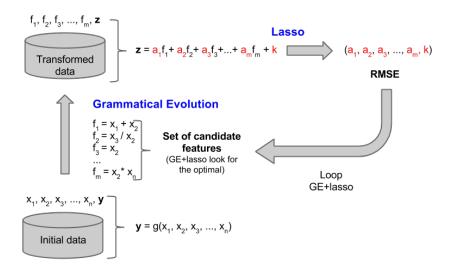


Fig. 2 Optimized modeling using GE+lasso methodology.

Each individual of the GE encodes its own set of candidate features $f_1, f_2, f_3, \ldots, f_m$. The candidate features follow the rules imposed by a BNF grammar allowing the occurrence of a wide variety of operations and operands to favor building optimal sets of features. Figure 3 shows an example of a BNF grammar for this approach.

Fig. 3 Grammar in BNF format. x variables, with $i = 0 \dots n$, represent each parameter obtained from the system.

This grammar provides the operations +, -, *, / and preoperators exp, sin, cos, ln. The space of solutions is easily modified by incorporating a broader set of relationships between operands to the BNF grammar.

The output of the GE stage consists of a matrix that includes all the candidate features provided by individuals. Each individual output vector has its own set of m candidate features that intends to minimize the fitness function provided for the system optimization.

$$\mathbf{z} = g_2(f_1, f_2, f_3, \dots, f_m) \tag{3}$$

4.2 Lasso generic model generation

Modeling procedures usually intend to interpret systems' behavior. They have the purpose of acquiring additional knowledge from the final models once these have been derived. Linearity, convexity and differentiability offered by lasso classic regression helps modeling to be a more explanatory and repeatable process. In addition, whereas GE is able to find complex symbolic expressions, GE does not perform well in parameter identification, mainly because the exploration of real numbers is not easily representable in BNFs. Due to these facts, we have included lasso algorithm in our methodology in order to manage the coefficient generation of the system model.

As can be seen in Figure 2, each individual of the GE provides a set of candidate features to *lasso*. This classical regression is in charge of deriving the optimized model for each individual by solving the following equation.

$$\mathbf{z} = a_1 f_1 + a_2 f_2 + a_3 f_3 + \dots + a_m f_m + k \tag{4}$$

Lasso offers the set of optimized coefficients $(a_1, a_2, a_3, \ldots, a_m, k)$ for each individual that minimizes the fitness function. This process provides the goodness of each individual. All this information feeds back the GE algorithm to generate the next population of individuals through selection, crossover and mutation, creating a loop. The loop continues executing until it completes the number of generations defined by the GE. This process results in the set of models that best fits system performance.

4.3 Fitness evaluation

As our main target is to build accurate models, our fitness function includes the error resulting in the estimation process. The fitness function presented in 5 leads the evolution to obtain optimized solutions thus minimizing Root Mean Square Error or RMSD.

$$F = \sqrt{\frac{1}{N} \cdot \sum_{n} e_{n}^{2}} \tag{5}$$

$$e_{n} = |P(n) - \widehat{P}(n)|, \qquad 1 \le n \le N \tag{6}$$

Estimation error e_n represents the deviation between the measure given by system monitoring P, and the estimation obtained by the model \widehat{P} . n represents each sample of the entire set of N samples used to train the algorithms.

5 Case Study

In this section we describe a particular case study for the application of the devised methodology presented in Section 4. The problem to be solved is the fast and accurate estimation of the power consumption in virtualized enterprise servers performing Cloud applications. Our power model considers heterogeneity of servers, as well as specific technological features and non-traditional parameters of the target architecture that affect power consumption. Hence, we propose our modeling technique that considers all these factors by combining the benefits of both GE algorithms and classical lasso regressions.

Firstly, a GE algorithm is applied to extract those relevant features that best describe power consumption sources. Features may also include correlations and combinations of representative variables due to FE performed by GE. Then, the *lasso* algorithm takes the optimal set of features in order to infer an expression that characterizes the power behavior of the target architecture of a Cloud server. As a result, we derive a highly accurate, linear and convex power model, targeting a specific server architecture, that is automatically generated by our evolutionary methodology.

We apply our methodology described in Section 4 to real measures gathered from a high-end Cloud server in order to infer an accurate power model. Also, we provide an experimental scenario for various workloads with the purpose of building and testing our methodology.

5.1 Data compilation

Data have been collected gathering real measures from a Fujitsu RX300 S6 server based on an Intel Xeon E5620 processor. This high-end server has a RAM memory of 16GB and is running a 64bit CentOS 6.4 OS virtualized by the QEMU-KVM hypervisor. Physical resources are assigned to four KVM virtual machines, each one with a CPU core and a 4GB RAM block.

The power consumption of a high-end server usually depends on several factors that affect both dynamic and static behavior [2]. Our proposed case study takes into account the following 7 variables:

- Ucpu: CPU utilization (%)
- Tcpu: CPU temperature (Kelvin)
- Fcpu: CPU frequency (GHz)
- Vcpu: CPU voltage (V)
- Umem: Main memory utilization (Memory accesses per cycle)
- Tmem: Main memory temperature (Kelvin)
- Fan: Fan speed (RPM)

Power consumption is measured with a current clamp with the aim of validating our approach. CPU and main memory utilization are monitored using hardware counters collected with *perf* monitoring tool. On board sensors are checked via IPMI to get both CPU and memory temperatures and fan speed. CPU frequency and voltage are monitored via *cpufreq-utils* Linux package. To build a model that includes power dependance with these variables, we use this software tool to modify CPU DVFS modes during workload execution. Also room temperature has been modified in run-time with the goal of finding non-traditional consumption sources that are influenced by this variable.

5.2 Experimental workload

We define three workload profiles (i) synthetic, (ii) Cloud and (iii) HPC over Cloud as they emulate different utilization patterns that could be found in typical Cloud infrastructures.

5.2.1 Synthetic benchmarks

The use of synthetic load allows to specifically stress different server resources. The importance of using synthetic load is to include situations that do not meet the actual real workloads that we have selected. Thus, the range of possible values of the different variables is extended in order to adapt the model to fit future workload characteristics and profiles. Lookbusy¹ stresses dif-

¹ http://www.devin.com/lookbusy/

ferent CPU hardware threads to a certain utilization avoiding memory or disk usage. The memory subsystem is also stressed separately using a modified version of $RandMem^2$. We have developed a program based on this benchmark to access random memory regions individually, with the aim of exploring memory performance. Lookbusy and RandMem have been executed, in a separated and combined fashion, onto 4 parallel Virtual Machines that consume entirely the available computing resources of the server.

On the other hand, real workload of a Cloud data center is represented by the execution of Web Search, from CloudSuite³, as well as by SPEC_CPU2006 mcf and SPEC_CPU2006 perlbench [19].

5.2.2 Cloud workload

Web Search characterizes web search engines, which are typical Cloud applications. This benchmark processes client requests by indexing data collected from online sources. Our Web Search benchmark is composed of three VMs performing as index serving nodes (ISNs) of Nutch 1.2. Data are collected in the distributed file system with a data segment of 6 MB, and an index of 2 MB that is crawled from the public Internet. One of this ISNs also executes a Tomcat 7.0.23 frontend in charge of sending index search requests to all the ISNs. The frontend also collects ISNs responses and sends them back to the requesting client. Client behavior is generated by Faban 0.7 performing in a fourth VM. Resource utilization depends proportionally on the number of clients accessing Web Search. Our number of clients configuration ranges from 100 to 300 to expose more information about the application performance. The four VMs use all the memory and CPU resources available in each server.

5.2.3 HPC over Cloud

In order to represent HPC over a Cloud computing infrastructure, we choose $SPEC_CPU2006\ mcf$ and perl-bench as they are memory and CPU-intensive, and CPU-intensive applications, respectively. $SPEC_CPU2006\ mcf$ consists on a network simplex algorithm accelerated with a column generation that solves large-scale minimum-cost flow problems. On the other hand, a mail-based benchmark is performed by $SPEC_CPU2006\ perlbench$. This program applies a spam checking software to randomly generated email messages. Both SPEC applications are run in parallel in 4 VMs using entirely the available resources of the server.

Instead of restricting the use of synthetic workloads only for training the algorithms, and limiting the use of real Cloud benchmarks exclusively for testing, we have used both workloads for the two purposes. This procedure provides automation for the progressive incorporation of additional benchmarks to the model.

For each run of the combined GE+lasso approach, we randomly select 50% of each data set (synthetic, Web Search, SPEC_CPU2006 mcf and perlbench) for training and the remaining 50% for testing stage. This technique validates the variability and versatility of the system, by analyzing the occurrence of local minima in optimization scenarios.

6 Experimental results

As we stated in section 5, tests have been conducted gathering real data from our Fujitsu server. Our experiments present high variability for the different features compiled from the server.

- CPU operation frequency (Fcpu) is fixed to $f_1 = 1.73$ GHz, $f_2 = 1.86$ GHz, $f_3 = 2.13$ GHz, $f_4 = 2.26$ GHz, $f_5 = 2.39$ GHz and $f_6 = 2.40$ GHz; thus modifying CPU voltage (Vcpu) from 1.73 V to 2.4 V.
- Room temperature has been modified in run-time, from 17°C to 27°C. Therefore, temperatures of CPU and memory (*Tcpu* and *Tmem*) range from 306 K to 337 K, and from 298 K to 318 K respectively.
- CPU and memory utilizations (*Ucpu* and *Umem*) take values from 0% to 100% and from 0 to 0.508 memory accesses (cache-misses) per CPU cycle respectively.
- Finally, due to both room temperature, and CPU and memory utilization variations, fan speed values (Fan) range from 3540 RPM to 7200 RPM.

Data have been split into training and testing sets. Training stage performs feature selection and builds the power model according to our grammar and fitness function. Next, the testing stage examines the power model accuracy. The algorithm proposed by our methodology is executed completely 20 rounds using the same grammar and fitness function configuration. For each run, we randomly select 50% of each data set for training and 50% for testing stage, thus obtaining 20 final power models. This procedure validates the variability and versatility of the system, by analyzing the occurrence of local minima in optimization scenarios.

 $^{^2\ \, \}rm http://www.roylongbottom.org.uk$

³ http://parsa.epfl.ch/cloudsuite

6.1 Algorithm setup

6.1.1 GE setup parameters

We use GE to obtain a set of candidate features that best describe our optimization problem. To obtain adequate solutions we tune the algorithm using the following parameters:

Population size: 250 individuals
Number of generations: 3000
Chromosome length: 100 codons

 Mutation probability: inversely proportional to the number of rules, 1/4 in our case.

Crossover probability: 0.9Maximum wraps: 3Codon size: 256

- Tournament size: 2 (binary)

As we strictly seek for simple combination of features, our proposed BNF grammar only provides the operations +|-|*|/. The space of solutions is easily increased by incorporating more complex relationships between operands to the BNF grammar. Figure 4 shows the BNF grammar proposed for this case study.

Fig. 4 Grammar in BNF format. x variables, with $i=0\ldots 6$, represent processor and memory temperatures, fan speed, processor and memory utilization percentages, processor frequency and voltage, respectively.

6.1.2 Lasso setup parameters

We use the *lasso* algorithm to obtain a set of candidate solutions with low error, when compared with the real power consumption measures in order to solve our optimization modeling problem. *Lasso* setup parameters are the following:

- Number of observations: 100
- λ regularization parameter: Geometric sequence of 100 values, the largest just sufficient to produce zero coefficients.
- $-\lambda$ regularization parameter: $1 \cdot 10^{-4}$

6.2 Training stage

We have performed variable standardization for every feature (in the range [1,2]) to assure the same probability of appearance for all the variables and to enhance the GE symbolic regression. Experiments with more than 4 features do not provide better values for RMSD. Hence, we have bounded their occurrence to a maximum of 4 by penalizing higher number of features in our fitness evaluation function. This also facilitates the generation of simpler models, which are faster and easy to be applied, in order to be used for realtime power optimizations. Table 1 shows phenotypes of each feature combined with the coefficients provided by lasso that are obtained for 20 complete executions of our methodology algorithm. Fitness results, that correspond to the RMSD between measured and estimated power consumption (see Equation 5), are shown in Table 2 for the training stage. Both Table 1 and Table 2 present the results for the best model of each execution.

As can be seen in Table 1, power model solutions combine features that correspond to a single variable with others that merge a combination of several parameters. On the one hand, there are single variable features that appear in up to 50% of the power model solutions. This shows that there are linear dependencies with certain parameters, as Ucpu, Tpcu, and Tmem that are consistent regardless of the workload that is used for training and testing. On the other hand, variables as Vcpu, Fcpu and Umem are seldom treated as a feature in the model solutions. However, they systematically appear when combined with other variables. These results show how there exist input parameters that are not relevant for the modeling or they are correlated to other features, and their inclusion could decrease the model accuracy. Model training for run 10 shows the lowest RMSD error of 0.1067.

6.3 Model testing

At this stage, we analyze the quality of the models that we have simultaneously tested for the 20 complete executions of our methodology algorithm. Results are also analyzed particularly for the testing data that corresponds to each benchmark dataset in order to verify the estimation reliability of the models for different workloads. Table 2 shows testing average error percentages particularized for the different benchmark data sets. These values have been obtained according to the following formulation:

$$e_{\text{AVG}} = \sqrt{\frac{1}{N} \cdot \sum_{n} \big(\frac{|P(n) - \widehat{P}(n)| \cdot 100}{P(n)}\big)^2}, 1 \leq n \leq N(7)$$

 $\textbf{Table 1} \ \ \text{Power models obtained by combining GE features and } \textit{lasso} \ \ \text{coefficients for 20 executions}$

Run 1	$a_1 \cdot f_1 + a_2 \cdot f_2 + a_3 \cdot f_3 + a_4 \cdot f_4 + K$ 0.288 · Tcpu
1	$+0.127 \cdot (((\text{Tcpu*Ucpu})-\text{Umem})*\text{Fan})$
	+ 0.220 · (Fan*Tmem)
	+ -0.450 · Fan + 1.043
2	0.173 · Ucpu
	$+ 0.438 \cdot \text{Tcpu}$
	+ -0.209 · Fan
0	$+0.070 \cdot (\text{Tmem/(Umem/(Fan*Tmem))}) + 0.636$
3	0.256 · (Fan/(Ucpu/Tmem))
	$+ 0.346 \cdot \text{Ucpu} + -0.694 \cdot (\text{Fan/Tcpu}) + 1.151$
4	-0.376 · Tmem
-	$+ -0.033 \cdot ((((Fan/Tcpu)/(Fcpu+Fcpu))/((Fan/(Vcpu+Umem))/Ucpu))*Fan)$
	$+0.606 \cdot ((Fan/((Umem+(Fan+(Fcpu/Fcpu)))*(Fan/Ucpu)))+(Fan+Tmem))$
	$+ 0.786 \cdot ((\text{Fcpu-(Fcpu+Fan)})/\text{Tcpu}) + 0.810$
5	0.181 · Ucpu
	$+0.254 \cdot (Fan*Tmem)$
	+ 0.378 · Umem
6	$+ -0.345 \cdot (((\text{Umem} + \text{Umem}) + \text{Fan})/\text{Tcpu}) + 0.939$ $0.483 \cdot (\text{Ucpu-Fan})$
U	$+0.030 \cdot ((Tmem+Fan)*((Fan-(Tmem/((Ucpu+Vcpu)+(Fan+Fan))))*(Fan*Fan)))$
	$+ 0.220 \cdot \text{Tmem}$
	$+ 0.430 \cdot (\text{Tcpu/Ucpu}) + 0.402$
7	0.506 · Tcpu
	$+ 0.195 \cdot ((Ucpu/(Vcpu+(Tmem-Umem)))*Vcpu)$
	+ -0.319 · Fan
	$+ -0.199 \cdot (((Fan + Umem)*((Umem - Tmem)/Tcpu))*Fan) + 0.704$
8	0.084 · (Ucpu/Vcpu)
	$+ 0.473 \cdot \text{Tmem}$ $+ 0.499 \cdot (\text{Ucpu/(Ucpu*(((Fcpu-Vcpu)+Tmem)/Tcpu))})$
	$+ 0.499 \cdot (\text{Ccpu}/(\text{Ccpu}/(\text{Ccpu}/(\text{Ccpu}/\text{Ccpu}) + 1 \text{mem})/(\text{1cpu})))) + 0.046$
9	0.927 · Ucpu
-	+ -0.380 · Fan
	$+0.232 \cdot (((Tmem*((Fan+Umem)-Ucpu))+(Tcpu-(Ucpu*Umem)))-Ucpu)$
	$+ 0.180 \cdot \text{Tcpu} + 0.365$
10	-0.073 · Tmem
	$+0.106 \cdot (((Tmem+Fan)*Fan)-Umem)$
	+ 0.194 · (Ucpu+Tmem)
11	$+0.437 \cdot (\text{Tcpu-Fan}) + 0.665$ $-0.117 \cdot (\text{Tmem}^*(\text{Ucpu-(Tmem}^*\text{Fan})))$
11	$+0.317 \cdot \text{Ucpu}$
	$+0.377 \cdot (\text{Tcpu-Fan}) + 0.810$
12	-0.070 · Umem
	$+ 0.174 \cdot \text{Ucpu}$
	$+ 0.647 \cdot (\text{Tcpu/Tmem})$
1.0	+ 0.647 · Tmem + -0.318
13	$0.291 \cdot (Tmem+Fan)$ + $-0.409 \cdot (Fan/Tcpu)$
	+ 0.234 · Tcpu
	$+ 0.423 \cdot (\text{Ucpu/(Tmem+Umem})) + 0.442$
14	$0.093 \cdot (\text{Ucpu} + (\text{Ucpu} + (\text{Tmem}*\text{Tmem})))$
	+ -0.019 · ((Tcpu-((Tmem*Fan)-Vcpu))-Vcpu)
	+ -0.081 · (Tmem+Umem)
	$+ 0.462 \cdot \text{Tcpu} + 0.526$
15	-0.004 · Fcpu
	$+ 0.380 \cdot (\text{Ucpu/(Umem+Fan)})$
	$+ 0.054 \cdot (Tmem*(Tmem+Fan)) + 0.454 \cdot Tcpu + 0.347$
16	-0.010 · Fan
	$+ -0.155 \cdot (((Fan/Tmem)-(Tmem/Ucpu))*Fan)$
	+ 0.282 · Ucpu
	$+ 0.417 \cdot \text{Tcpu} + 0.393$
17	$0.242 \cdot (Fan*(Tmem/Ucpu))$
	$+ 0.396 \cdot (\text{Tcpu-Fan})$
	+ 0.001 · Fcpu
10	+ 0.344 · Ucpu + 0.508
18	$0.448 \cdot \text{Tmem} + -0.178 \cdot \text{Umem}$
	+ -0.178 · Official $+$ -0.221 · (((((Tcpu/(Vcpu/(Fcpu-Vcpu)))-Ucpu)+Fan)/Tmem)-(Tcpu-(Tmem-(Tcpu+Fan))))
	$+ 0.100 \cdot (\text{Umem/Fan}) + 0.271$
19	0.134 · Ucpu
	$+0.241 \cdot (\text{Tmem*Fan})$
	$+~0.066 \cdot \mathrm{\dot{U}cpu}$
	$+ -0.403 \cdot ((Fan-Tcpu)/Umem) + 0.653$
20	$-0.433 \cdot (((Fan-(Ucpu+Umem))/Fan)-(Tcpu+Fan))$
	+ -0.295 · Umem
	1 0 100 Fee
	$+ -0.102 \cdot \text{Fan} + 0.235 \cdot (((\text{Tmem-Umem})-\text{Ucpu})+\text{Fan}) + 0.184$

Table 2	RMSD	and	Average	testing	error	percentages	for 20	executions

Run	Train (RMSD)	Validation (RMSD)	Synthetic (%)	mcf (%)	perlb (%)	WebSearch (%)	Total (%)
1	0.1069	0.1068	3.985	4.097	4.463	4.147	4.173
2	0.1068	0.1067	3.984	4.099	4.463	4.110	4.164
3	0.1070	0.1068	3.995	4.110	4.504	4.145	4.189
4	0.1070	0.1071	4.007	4.085	4.469	4.155	4.179
5	0.1069	0.1069	3.991	4.106	4.494	4.113	4.176
6	0.1071	0.1068	3.988	4.085	4.459	4.153	4.171
7	0.1070	0.1072	3.995	4.042	4.462	4.101	4.150
8	0.1071	0.1072	3.994	3.996	4.559	4.101	4.162
9	0.1072	0.1072	4.033	3.884	3.990	4.059	3.991
10	0.1067	0.1072	4.052	3.894	3.969	4.031	3.986
11	0.1073	0.1075	4.023	3.926	3.963	4.063	3.994
12	0.1071	0.1076	4.098	3.896	3.951	4.030	3.994
13	0.1070	0.1070	4.073	3.939	4.173	4.243	4.107
14	0.1072	0.1072	4.088	3.935	4.174	4.184	4.096
15	0.1071	0.1070	4.083	3.922	4.161	4.246	4.103
16	0.1071	0.1070	4.060	3.937	4.164	4.217	4.095
17	0.1079	0.1057	3.951	4.136	4.208	4.056	4.088
18	0.1081	0.1060	3.981	4.171	4.180	4.050	4.095
19	0.1082	0.1060	3.953	4.190	4.224	4.212	4.145
20	0.1082	0.1059	3.974	4.205	4.178	4.074	4.108

where P is the power measure given by the current clamp and \widehat{P} is the power estimated by the model phenotype. n represents each sample of the entire set of N samples.

Total average error for the testing dataset shows lowest error of 3.98% (as shown in Table 2). Best testing error corresponds to the solution with lower training error. Solutions can be broken down for those samples that belong to different tests, achieving testing errors of 4.052%, 3.894%, 3.969% and 4.031% for synthetic, SPEC_CPU2006 mcf, SPEC_CPU2006 perlbench and WebSearch workloads respectively. This fact confirms that our methodology works well for our scenario, extracting optimized sets of features and coefficients that are consistent even for 20 runs with random selection of both training and testing dataset.

Our methodology application shows very accurate testing results for all of the whole executions ranging from 3.98% to 4.18%. The obtained results are robust, as they have been obtained for a heterogeneous mix of workloads so the power models are not workload-dependant. According to these results, we can infer that our methodology is effective for performing feature selection and building accurate multi-parametric, linear, convex and differentiable power models for highend Cloud servers. This technique can be considered as a starting point for implementing energy optimization policies for Cloud computing facilities.

7 Conclusions

This paper has presented a novel work in the field of FE and SR for the automatic inference of accurate models.

Resulting models include combination and correlation of variables due to the FE and SR performed by GE. Therefore, the models incorporate the optimal selection of representative features that best describe the target problem while providing linearity, convexity and differentiability characteristics.

As a proof of concept, the devised methodology has been applied to a current computing problem, the power modeling of high-end servers in a Cloud environment. In this context, the proposed methodology has shown relevant benefits with respect to state-of-the-art approaches, like better accuracy and the opportunity to consider a broader number of input parameters that can be exploited by further power optimization techniques.

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