Fast $CP$ violation

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$B$ flavor tagging will be extensively studied at the asymmetric $B$ factories due to its importance in $CP$ asymmetry measurements. The primary tagging modes are the semileptonic decays of the $b$ (lepton tag), or the hadronic $b \rightarrow c (\rightarrow s)$ decays (kaon tag). We suggest that looking for time dependent $CP$ asymmetries in events where one $B$ is tagged leptonically and the other one is tagged with a kaon could result in an early detection of $CP$ violation. Although in the standard model these asymmetries are expected to be small, $\sim 1\%$, they could be measured with about the same amount of data as in the “gold-plated” decay $B_d \rightarrow \phi K_S$. In the presence of physics beyond the standard model, these asymmetries could be as large as $\sim 5\%$, and the first $CP$ violation signal in the $B$ system may show up in these events. We give explicit examples of new physics scenarios where this occurs. [S0556-2821(98)09321-7]

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I. INTRODUCTION

One of the goals of the asymmetric $B$ factories is to study $CP$ violation in $B$ meson decays. $CP$ violation has not been observed outside the kaon system; thus it is important to identify $B$ decay modes that would allow an early detection of this phenomenon. The $CP$ asymmetry in the $B_d \rightarrow \phi K_S$ decay is the benchmark to which all other $CP$ asymmetry measurements at the $B$ factories are usually compared [1]. The branching ratio is relatively large ($5 \times 10^{-4}$) and the $\phi$ is easy to reconstruct from its decay into two leptons. In addition, the $CP$ asymmetry is expected to be $O(1)$ in the standard model, and will allow a clean measurement of the Cabibbo-Kobayashi-Maskawa (CKM) angle $\beta$. It is also commonly assumed that this is the mode in which $CP$ violation will first be observed at the asymmetric $B$ factories.

A crucial ingredient in the $CP$ asymmetry measurements is flavor tagging. In the asymmetric $B$ factories there are two main tagging techniques [2]. The first is the “lepton tag,” where the flavor is determined by the lepton charge in a semileptonic $B$ decay. The second, the “kaon tag,” uses hadronic $B_d$ decays to final states with $\Delta C = \pm 1$, namely decays with one charmed hadron in the final state. These further decay into a final state that contains only one kaon, whose charge identifies the original $B$ meson flavor.

In this work we propose that $CP$ asymmetries in events where both $B$’s are flavor tagged are also excellent candidates for an early observation of $CP$ violation. The cases where both $B$’s are tagged leptonically or both with kaons result in $CP$ asymmetries that are proportional only to $CP$ violation in the $B^0 - \bar{B}^0$ mixing amplitude and, in particular, they vanish in the limit where the neutral $B$ width difference, $\Delta \Gamma$, is zero. The case we concentrate on here is where one of the $B$’s is tagged leptonically and the other using the kaon tag. This can lead to $CP$ violation due to interference between the neutral $B$ mixing and decay amplitudes. Theoretically, these are given by the $CP$ asymmetries in hadronic semi-inclusive $B_d$ decays to final states with $\Delta C = \pm 1$. Because of the importance of the kaon tag to the $B$ factories program, the experimental issues regarding the detection of these final states will be extensively studied before and after the $B$ factories turn on. Moreover, the search for these states should not result in much additional effort since it will be carried out when performing the tagging. Thus, we believe that the possibility of an early detection of $CP$ violation in these modes requires a simple extension of the flavor tagging studies.

The $CP$ asymmetries we consider are the following:

\begin{eqnarray}
 a_{C=+1}(t) &=& \frac{N_{B_b \bar{B}_K(t)} - N_{\bar{B}_b \bar{B}_K(t)}}{N_{B_b \bar{B}_K(t)} + N_{\bar{B}_b \bar{B}_K(t)}}, \\
 a_{C=-1}(t) &=& \frac{N_{B_b \bar{B}_K(t)} - N_{\bar{B}_b \bar{B}_K(t)}}{N_{B_b \bar{B}_K(t)} + N_{\bar{B}_b \bar{B}_K(t)}}, \\
 a_{\Delta C=1}(t) &=& \frac{(N_{B_b \bar{B}_K(t)} + N_{B_\bar{B}_K(t)}) - (N_{\bar{B}_b \bar{B}_K(t)} + N_{\bar{B}_\bar{B}_K(t)})}{(N_{B_b \bar{B}_K(t)} + N_{B_\bar{B}_K(t)}) + (N_{\bar{B}_b \bar{B}_K(t)} + N_{\bar{B}_\bar{B}_K(t)})}.
\end{eqnarray}

In the above notation $N_{B_b \bar{B}_K}$ is the number of events where a $B$ has been tagged leptonically and a $\bar{B}$ has been tagged with a kaon ($N_{\bar{B}_b \bar{B}_K}$ and $N_{B_\bar{B}_K}$ are similarly defined). As we will show, in the standard model, the number of $B^0 - \bar{B}^0$ pairs required to get a statistically significant $CP$ violation signal in $B_d \rightarrow \Delta C = \pm 1$ is expected to be larger than that required in $B_d \rightarrow \phi K_S$, yet achievable in approximately one year of data taking at nominal luminosity. If, however, there is physics beyond the standard model, it could lead to the possibility of observing $CP$ violation in $B_d \rightarrow \Delta C = \pm 1$ in the very early stages of data taking, with up to an order of magnitude fewer $B^0 - \bar{B}^0$ events than those needed for the $CP$ asymmetry in $B_d \rightarrow \phi K_S$. 

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II. FORMALISM AND STANDARD MODEL EXPECTATIONS

The suggestion of looking for a CP asymmetry in the semi-inclusive $B_d \rightarrow \Delta C = \pm 1$ modes, the formalism to calculate it, as well as the standard model expectations were presented in a recent paper by Beneke, Buchalla and Dunietz [3]. Ignoring the width difference of the neutral $B$ mesons ($\Gamma_{1s}/M_{1s} = 0$), one obtains

$$a^{SM}_{\Delta C = \pm 1}(t) = \frac{2 \text{ Im } \lambda_{SM} \sin \Delta mt}{(1 + \cos \Delta mt) + |\lambda_{SM}|^2 (1 + \cos \Delta mt)},$$

and

$$a^{SM}_{|\Delta C| = 1}(t) = C \times 2 \text{ Im } \lambda_{SM} \sin \Delta mt,$$

where $\lambda_{SM} = e^{i2\beta} (V_{ub} V_{cb}^*)/(V_{ub} V_{cd})$ and $C$ is a dilution factor that arises because one is summarizing over several exclusive modes, possibly with opposite CP asymmetries. Assuming local quark-hadron duality, setting all bag factors equal to one, and using $f_B = 180 \text{ MeV}$, $m_f = 4.8 \text{ GeV}$ and $m_r = 1.4 \text{ GeV}$, one finds $C = -0.21$ [3]. Using $|V_{ub}|/|V_{cb}| = 0.1$ one then obtains

$$a^{SM}_{\Delta C = \pm 1}(t) \approx -0.01 \sin(\alpha - \beta) \sin \Delta mt / (1 + \cos \Delta mt) + 0.0005(1 + \cos \Delta mt),$$

and

$$a^{SM}_{|\Delta C| = 1}(t) \approx -0.01 \sin(\alpha - \beta) \sin \Delta mt.$$

For comparison, the CP asymmetry in $B_d \rightarrow \psi K_S$ is given by

$$a^{SM}_{\psi K_S}(t) = \sin(2\beta) \sin \Delta mt,$$

with essentially no uncertainty. We consider the value of $C$ used above only as a reasonable estimate due to the large uncertainties in some of the factors that go into its determination. Until these are better known, the CP asymmetries in Eqs. (2.3) and (2.4) are unlikely to be of much use in obtaining precise measurements of CKM angles, as suggested in [3]. The importance of these modes lies, rather, in the fact that they may lead to an early detection of CP violation; possibly the first at the $B$ factories.

The number of $B^0 - \bar{B}^0$ events needed to establish CP violation depends not only on the expected CP asymmetry, but also on the $B$ meson branching ratio as well as on tagging and detection efficiencies for that particular final state. Thus, the small CP asymmetry in $B_d \rightarrow \Delta C = \pm 1$ is compensated for by the large branching ratio into these modes. We can estimate the number of $B^0 - \bar{B}^0$ pairs ($N_f$) required to obtain a $3\sigma$ CP violation signal in a given final state $f$ using

$$N_f \epsilon_f \text{ BR}_f \approx \frac{10}{a_f},$$

where $\epsilon_f$ is the combination of detection and $B$ flavor tagging efficiencies, $\text{BR}_f$ the branching ratio, and $a_f$ is a time integrated CP asymmetry for the final state $f$. We present below the results based on Eq. (2.6) for the various modes, relegating details concerning its implementation to the Appendix.

For the $\Delta C = \pm 1$ modes we find, in the standard model,

$$N_{|\Delta C| = 1} \approx \frac{2 \times 10^7}{\sin^2(\beta - \alpha)},$$

$$N_{\Delta C = \mp 1} \approx \frac{2 \times 10^7}{\sin^2(\beta - \alpha)},$$

$$N_{\Delta C = 0} \approx \frac{6 \times 10^7}{\sin^2(\beta - \alpha)}.$$

For comparison, the number of $B^0 - \bar{B}^0$ pairs needed to establish a CP violation in $B_d \rightarrow \psi K_S$ can be estimated to be about

$$N_{\psi K_S} \approx \frac{3 \times 10^6}{\sin^2(2\beta)}.$$

Thus, one can expect to observe CP violation in the $B_d \rightarrow \Delta C = \pm 1$ modes with roughly an order of magnitude more data than that needed in the “gold-plated” $B_d \rightarrow \psi K_S$ mode. This amount of data will be available after one to two years of data taking with the expected luminosity yielding $\sim 10^7 B^0 - \bar{B}^0$ pairs per year. If it turns out that $|\bar{C}| > 0.21$ or if $|\sin(\alpha - \beta)| > |\sin(2\beta)|$, it may be possible to observe CP violation in the $B_d \rightarrow \Delta C = \pm 1$ modes with a comparable amount of data as in $B_d \rightarrow \psi K_S$ even in the standard model. Given the fact that, in any case, data will be taken and analyzed in the $B_d \rightarrow \Delta C = \pm 1$ modes, it is important then to also search for CP violation.

III. NEW PHYSICS

The situation gets even more interesting in the presence of physics beyond the standard model. Note from Eq. (2.6) that $N_f$ scales as $(a_f)^{-2}$, and that the small value of $(a_{\Delta C = \pm 1})$ in Eqs. (2.3) and (2.4) is essentially due to the small ratio of amplitudes,

$$\left| \frac{A(b \rightarrow u\bar{c}d)}{A(b \rightarrow c\bar{u}d)} \right|_{SM} = \lambda \frac{|V_{ub}|}{|V_{cb}|}.$$

However, the $b \rightarrow u\bar{c}d$ rate is not well measured at present and could contain large CP violating new physics contributions. If such new contributions significantly enhance the magnitude of that amplitude, they will also enhance the CP asymmetries in these modes.

Let us first present a model independent analysis of the bounds on physics beyond the standard model for the $b \rightarrow u\bar{c}d$ transition. We parametrize the new physics effects by the quantity

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respectively, where $\theta$ is the phase between $A(b\to u\bar{c}d)_{NP}$ and $A(b\to u\bar{c}d)_{SM}$. Moreover, we have included the term proportional to $a_{SL} \approx \text{Im}(\Gamma_{12}/M_{12})$ [3] which is a measure of the $CP$ violation in events with two lepton tags, i.e.

$$\frac{N_{B,p}(t)-N_{\bar{B},p}(t)}{N_{B,p}(t)+N_{\bar{B},p}(t)} = a_{SL} \sin^2 \Delta mt \frac{\Delta mt}{2}, \quad (3.6)$$

and we are using the same notation as in Eqs. (1.1)–(1.3). This is expected to be negligible in the standard model, but is likely to get large enhancements from a new $b\to u\bar{c}d$ amplitude. Thus, we see that for $r \approx 5$ the $CP$ asymmetry can be enhanced by a factor of 5, and hence a $CP$ violation signal can be obtained with a factor 25 less data than required in the standard model. Note that since we care only about order of magnitude estimates, we have ignored corrections associated with generalizing the results of [3] to account for operators with non-standard Lorentz structures.

We now present constraints on the new physics contributions if it consists of right-handed currents contributing to the $b\to u\bar{c}d$ decay. There are no reported bounds on either the inclusive or exclusive decays. In order to derive such a constraint, we require that the branching ratio for this mode should not be large enough to have a significant effect on the $B$ semi-leptonic branching ratio. This implies $\text{BR}(b\to u\bar{c}d) \approx 10\%$. Comparing to the standard model expectation $\text{BR}(b\to u\bar{c}d)_{SM} \approx 1 \times 10^{-4}$ we obtain $r \approx 30$.

Considerations of exclusive decays also lead to similar bounds. For example, $r \approx 10$ combined with $\text{BR}(B^+ \to D^0 \rho^+) \approx 0.5\%$ leads to $\text{BR}(B^+ \to D^0 \pi^+) \approx 1.2 \times 10^{-4}$. Although CLEO has no bounds on this process, it is likely that a dedicated search could obtain a bound $\text{BR}(B^+ \to D^0 \pi^+) \approx 10^{-4}$. A larger enhancement up to $\text{BR}(B^+ \to D^0 \pi^+) \approx 10^{-3}$ is unlikely, as this might result in intrinsic inconsistencies in other measurements such as $B \to DK$ [7].

Finally, this new amplitude could result in a large enhancement of the semi-leptonic $CP$ asymmetry $a_{SL}$ essentially because it makes a large contribution to final states common to both $B^0$ and $\bar{B}^0$ mesons, and moreover the Glashow-Iliopoulos-Maiani (GIM) mechanism which further suppresses the standard model result is no longer effective. If this new physics effect dominates $\Gamma_{12}$ one can derive the bound $a_{SL} \approx 0.015|r|$. Using OPAL’s 2$\sigma$ limit, $a_{SL} \approx 0.08$ [8], one obtains the constraint $r \approx 5$. Note, however, that this bound could be modified by a factor of a few if there are new contributions to $M_{12}$.

As a simple example of a new physics scenario that can lead to such large values of $r$, and thus enhanced $CP$ violation in $B_d \to \Delta C = \pm 1$, we consider a nonminimal left-right symmetric model [9]. Namely, one where the left ($V^L$) and right ($V^R$) quark mixing matrices are not related. We assume identical gauge couplings, $g_L = g_R$, and that the $W_L - W_R$ mixing is negligible. Then, tree level $W_R$ exchange can lead to the desired final state. The ratio of the new amplitude to the standard model one is

$$|r| \approx \frac{V^R_{ub}V^R_{cd}}{V^R_{ub}V^L_{cd}} \frac{m_{W_L}^2}{m_{W_R}^2}. \quad (3.7)$$

For $|V^R_{ub}V^R_{cd}| \approx 1/2$ and $m_{W_R} \approx 10m_{W_L}$ we get $r \approx 5$, while still satisfying all other constraints on the model. Of course, we also assume that the $CP$ violating phase in $V^R$ is large, $O(1)$.

In this case the $CP$ asymmetries in the various tagging modes are enhanced and can reach the 5% level. As a consequence, we would observe a $CP$ violation signal in events with one lepton and one kaon tag, as well as in events with

\[ A(b\to u\bar{c}d)_{NP} = \frac{a_{SL}}{A(b\to u\bar{c}d)_{SM}}. \quad (3.2) \]
both lepton or both kaon tags with about $10^6 B^0 - \bar{B}^0$ pairs. Moreover, such enhanced $CP$ violation would be a clear signal of physics beyond the standard model. Of course, if no such signal is found, we will be able to put bounds on the magnitude of new contributions to the $b \to u \bar{c} d$ amplitude.

We have also studied other scenarios, e.g., models with extra charged scalars, models with diquarks, supersymmetry with four generations and broken $R$ parity, all of which allow $r \sim 5$, and hence the possibility of an early detection of $CP$ violation.

**IV. CONCLUSIONS**

We have proposed that it is important to search for $CP$ violation in events where one $B$ has been tagged leptonically, and the other $B$ by a kaon. Within the standard model, the number of $B^0 - \bar{B}^0$ events required to detect $CP$ violation in this mode could be similar to that for $B_d \to \psi K_S$, and could be obtained in the first year of running at the $B$ factories. In the presence of new physics, it is possible that $CP$ violation could be detected in $B_d \to \Delta C = \pm 1$ with significantly less data than needed to detect it in $B_d \to \psi K_S$, and thus be the first $CP$ violating signal at the asymmetric $B$ factories. Moreover, such new physics is likely to contribute to the $CP$ violation in events where one $B$'s are tagged either leptonically, or with kaons. Given the fact that $B$ flavor tagging will be intensively studied, we suggest that the possibility of observing $CP$ violation in these modes should be seriously considered.

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**APPENDIX: NUMERICAL ESTIMATES**

The number of $B^0 - \bar{B}^0$ pairs required to obtain a statistically significant observation of $CP$ violation has been estimated in the text by means of

$$N_f \epsilon_f \mathrm{BR}_f \simeq \frac{10}{\epsilon_f}$$

with

$$\mathcal{N}_f(t) = \Gamma(B(t) \to f) - \Gamma(\bar{B}(t) \to \bar{f}),$$

$$D_f(t) = \Gamma(B(t) \to f) + \Gamma(\bar{B}(t) \to \bar{f}).$$

Moreover, the number of neutral $B$ decays are an oscillatory function of time, and hence we use

$$\mathrm{BR}_f \approx \frac{\int_0^\infty D_f(t) dt}{2\Gamma}$$

where $\Gamma$ is the total $B$ width, finally leading to

$$N_f \approx \frac{20\Gamma}{\epsilon_f} \frac{\int_0^\infty D_f(t) dt}{(\int_0^\infty \mathcal{N}_f(t) dt)^2}.$$ 

Here we are assuming that we have already reconstructed the time information of the decay, since otherwise we could not make the $\int_0^\infty$ integral. Although in practice the $CP$ violating signal is best extracted by using all the data to perform a maximal likelihood fit to Eqs. (2.1) and (2.2), or their generalizations in the case of physics beyond the standard model, we believe that the above equation yields a reasonable estimate of the number of $B^0 - \bar{B}^0$ pairs required to see a $CP$ violating signal.

Using the information in the BABAR Technical Design Report, and recent studies made for the BABAR physics book [2], we estimate $\epsilon_{\Delta C = 1} \approx 2.5 \times 10^{-2}$ for all the $\Delta C = 1$ modes. This estimate is a product of 10% for the lepton tag, 50% for the kaon tag and a further 50% due to the fact that in the inclusive decay one needs to identify both the flavor and the charge of the decaying $B$. Similarly, we estimate $\epsilon_{\psi K_S} \approx 1.5 \times 10^{-2}$ as a product of 30% for the combined lepton and kaon tags, 10% for the $\psi$ reconstruction, and 50% for the $K_S$ reconstruction. We have ignored other possible systematic differences in observing the $CP$ asymmetries in the two modes such as the fact that the vertexing efficiencies may be different in the two cases, or that the purity required of the kaon tag may be different. We deem these to be subjects for a more detailed analysis than undertaken here.

When doing the integral in Eq. (A5) we utilize a common lower limit of 0.6 ps corresponding to a resolvable separation of 100 $\mu$m for the two $B$'s in the BABAR environment, and optimize the upper bound to get the best $CP$ signal. The $\Delta C = +1$ mode is particularly sensitive to the vertexing resolution since the smallness of the $D(t)$ at early times [cf. Eq. (2.1)] combined with the lack of exponential suppression from the $B$ lifetime, implies that one could significantly enhance the $CP$ signal by giving more weight to the early time region.