Galaxy classification: deep learning on the OTELO and COSMOS databases

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ABSTRACT

Context. The accurate classification of hundreds of thousands of galaxies observed in modern deep surveys is imperative if we want to understand the universe and its evolution.

Aims. Here, we report the use of machine learning techniques to classify early- and late-type galaxies in the OTELO and COSMOS databases using optical and infrared photometry and available shape parameters: either the Sérsic index or the concentration index.

Methods. We used three classification methods for the OTELO database: (1) a color–magnitude–shape parameter classification, and (3) a deep neural network using the r magnitude, several colors, and a shape parameter. We analyzed the performance of each method by sample bootstrapping and tested the performance of our neural network architecture using COSMOS data.

Results. The accuracy achieved by the deep neural network is greater than that of the other classification methods, and it can also operate with missing data. Our neural network architecture is able to classify both OTELO and COSMOS datasets regardless of small differences in the photometric bands used in each catalog.

Conclusions. In this study we show that the use of deep neural networks is a robust method to mine the cataloged data.

Key words. galaxies: general – methods: statistical

1. Introduction

Galaxy morphological classification plays a fundamental role in descriptions of the galaxy population in the universe, and in our understanding of galaxy formation and evolution. Galaxy morphology is related to key physical, evolutionary, and environmental properties, such as system dynamics (Djorgovski & Davis 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlot 2003; Kennicutt 1987; Gerhard et al. 2001; Debattista et al. 2006; Falcón-Barroso et al. 2019; Romanowsky & Fall 2012), the stellar formation history (Kennicutt 1998; Bruzual & Charlo
procedures have been implemented in extragalactic surveys such as for example COSMOS (Cassata et al. 2007; Zamojski et al. 2007) and GAMA (Alpaslan et al. 2015). Another approach involves the fitting of spectral energy distributions (SEDs) using galaxy templates (Ilbert et al. 2009). In a complementary fashion, Strateva et al. (2001) investigated the dichotomous classification in early- and late-type (ET and LT) galaxies. For these authors, the ET group includes the E, S0, and Sa morphological types, while the LT group comprises Sb, Sc, and Ir galaxies. Furthermore, using the well-known tendency of the LT to be bluer than the ET galaxies, Strateva et al. (2001) propose the $u - r$ color to separate between these galaxy types. Sérsic and concentration indexes have also been used, alone or in combination with the $u - r$ color, to separate ET from LT galaxies (e.g., Conselice 2003; Kelvin et al. 2012; Deng 2013; Vika et al. 2015). A far more complicated and expensive classification, in terms of computational and observational resources, consists in fitting a set of either empirical or modeled SED templates to the galaxy continuum (e.g., Cote et al. 1996; Kinney et al. 1996). Currently, there are some public codes that are able to perform such template-based classifications (e.g., LePhare: Arnouts et al. 1999; Ilbert et al. 2006).

Classification can be addressed in machine learning through supervised learning techniques, which consist in training a function that maps inputs to outputs learning from input–output pairs, and using this function to assign new observations in two or more predefined categories. Supervised learning techniques include decision trees (Barchi et al. 2020), random forests (Miller et al. 2017), linear discriminant analysis (LDA; Murtagh & Heck 1987), support vector machines (Huertas-Company et al. 2008), Bayesian classifiers (Henríon et al. 2011), and neural networks (Ball et al. 2004), among others.

Machine learning algorithms are increasingly used for classification in large astronomical databases (e.g., Abolfathi et al. 2018). In particular, LDA is a common classifying method used in statistics, pattern recognition, and machine learning. Linear discriminant analysis classifiers attempt to find linear boundaries that best separate the data. Recently, LDA has been using for galaxy classification in spiral and elliptical morphological types (Ferrari et al. 2015), classification of Hickson’s compact groups of galaxies (Abdel-Rahman & Mohammed 2019), and galaxy merger identification (Nevin et al. 2019).

In recent years, neural networks have become very popular in different research areas because of their ability to perform outstanding accurate classifications, and regression and series analyses. A typical neural network is made up of a number of hidden layers, each with a certain quantity of neurons that perform tensor operations. There are several network types which are oriented to solve different issues (a brief explanation of different networks can be found in Baron 2019). Also, Busca & Balbi (2018) develop a convolutional neural network (CNN) for classification and redshift estimates of quasar spectra extracted from the BOSS. Most of the recent research has focused on two-dimensional CNN classification of galaxy images (e.g., Serra-Ricart et al. 1996; Huertas-Company et al. 2015; Dieleman et al. 2015; Domínguez Sánchez et al. 2018; Pérez-Carrasco et al. 2019; Walmsley et al. 2020).

In the future, neural networks will probably gain more importance and become the primary technique for classification of astronomical images. However, there are two drawbacks that limit the use of CNN in astronomical research at present. The first is the network bandwidth, which prevents the download of large amounts of heavy images obtained in remote observatories. The second drawback is the computational and hardware resources needed to train a two-dimension CNN with tens of thousands of images.

Dense (or fully connected) neural networks (DNN) are used to solve general classification problems applied to tabulated data. In astronomy, DNNs have been applied to morphological type classification in low-redshift galaxies. Thus, Storrie-Lombardi et al. (1992) designed a simple DNN architecture for morphological classification of 5217 galaxies drawn from the ESO-LV catalog (Lauberts & Valentijn 1989) using 13 parameters (most of them geometrical) in five different classes, obtaining an accuracy of 56%. Naim et al. (1995) used the same architecture for 830 bright galaxies ($B \leq 17$) and 24 parameters, reducing the parameter space dimension through principal components analysis. Serra-Ricart et al. (1993) used DNN autoencoders for unsupervised classification of galaxies into three major classes: Sa+Sb, Sc+Sd, and SO+E. Sreejith et al. (2018) applied a DNN to a sample of 7528 galaxies at redshifts $z < 0.06$ extracted from the Galaxy And Mass Assembly survey (GAMA)\(^2\) achieving an accuracy of 89.8% for spheroid- versus disk-dominated classification.

These earlier works showed that DNNs are capable of performing accurate classification tasks on processed data such as photometry, colors, and shape parameters of low-redshift galaxies (Storrie-Lombardi et al. 1992; Naim et al. 1995; Ball et al. 2004). However, compared with image-oriented CNNs, little attention has been paid recently to the use of DNNs for galaxy classification, even if these networks do not require the large quantity of resources used by the CNN. Moreover, both neural network software development (e.g., Tensorflow, Abadi et al. 2016) and hardware computation power (both central and graphics processing units) have increased dramatically, boosting the capabilities of DNN applications.

In this paper we extend the use of DNNs to the morphological classification of galaxies up to redshifts $z \leq 2$. We compare the performance of different galaxy classification techniques applied to a sample of galaxies extracted from the photometric OTELO database (Bongiovanni et al. 2019) with a fitted Sérsic profile (Nadolny et al. 2020). These techniques are (1) the Strateva et al. (2001) $u − r$ color algorithm; (2) the LDA machine learning algorithm, which includes both the $u − r$ color and a shape parameter, either the Sérsic index or the concentration index (Kelvin et al. 2012); and (3) a DNN that uses optical and near-infrared photometry, and shape parameter for objects available in both OTELO and COSMOS catalogs. We find that a simple, easily trainable DNN yields a highly accurate classification for ET and LT OTELO galaxies. Moreover, we apply our DNN architecture to a set of tabulated COSMOS data with some differences in the photometric bands measured with respect to OTELO, and find that our architecture also performs accurate classification of COSMOS galaxies. Finally, we use the same DNN architecture but substituting the Sérsic index with the concentration index (Shimasaku et al. 2001) for both OTELO and COSMOS datasets.

This paper is organized as follows. Section 2 describes the different techniques used to classify galaxies. In Sect. 3 we show the results and compare the different techniques. Finally, in Sect. 4 we present our conclusions.

2. Methodology

The current investigation involves the automatic classification of galaxies into two dichotomous groups, namely ET and LT resources.
galaxies, using both photometric measurements and a factor that depends on the shape of the galaxies’ light distribution. Machine learning algorithms for automatic classification parse data and learn how to assign subjects to different classes. These algorithms require both training and test datasets that consist of labeled data. The training dataset is used to fit the model parameters, and the test dataset to provide an unbiased assessment of the model performance. If the algorithm requires tuning the model hyperparameters, such as the number of layers and hidden units in a DNN architecture, a third labeled dataset called the validation dataset is required to evaluate different model trials (the test dataset must be evaluated only by the final model). Once the final model architecture is attained, it is trained joining both the training and the validation dataset, and then evaluated using the test dataset.

In this section we present our samples of galaxies extracted from OTELO and COSMOS. We use the observed photometry and colors, that is, neither k nor extinction corrections were performed. In order to maximize the sample size while keeping a well-sampled set in redshift, data have been limited in photometric redshift ($z_{\text{phot}} \leq 2$) but not in flux, thus no cosmological inferences can be performed from our sample. However, at the end of Sect. 3 we present a brief analysis of the results obtained for flux-limited samples. We describe the photometry and the shape factors of these data. We then present the implementation of the different classification methodologies used: the k color, LDA, and DNN. Finally, we present the bootstrap procedure that we use to compare the results obtained with these methodologies.

2.1. OTELO samples

OTELO is a very deep blind survey performed with the red tunable filter OSIRIS instrument of the 10.4 m Gran Telescopio Canarias (Bongiovanni et al. 2019). OTELO data consist of images obtained in 36 adjacent narrow bands (FWHM 12 Å) covering a window of 230 Å around $\lambda = 9175$ Å. The catalog includes ancillary data ranging from X-rays to far infrared. Point spread function-model photometry and library templates were used for separating stars, AGNs, and galaxies.

The OTELO catalog comprises 11 237 galaxies. Nadolny et al. (2020) matched OTELO with the output from GALAPAGOS2 (Häussler et al. 2007; Häußler et al. 2013) over high-resolution HST images. Not all the OTELO galaxies were detected by GALAPAGOS2, which returned a total of 8812 sources. Nadolny et al. (2020) account for automated detection of multiple matches produced by more than one source that lay inside the OTELO’s Kron radius in a high-resolution F814W band image. These latter authors attribute these multiple matches to close companions (gravitationally bounded or in projection), mergers, or resolved parts of the host galaxy. In any case, sources with multiple matches were excluded from our analysis because they could affect low-resolution photometry. Finally, we included further constraints to extract our OTELO samples (see below).

2.1.1. Sérsic index and photometry sample

OTELO uses LePhare templates to fit the SED of galaxies to obtain photometric morphological type classification and redshift estimates. We used this morphological classification to assign the galaxies to ET and LT classes. The best model fitting is recorded under the MOD_BEST_deepN numerical coded entries in the OTELO catalog (Bongiovanni et al. 2019). The ET class includes galaxies coded as “1” in the OTELO catalog, which were best fitted by the E/S0 template from Coleman et al. (1980). The LT class comprises OTELO galaxies coded from “2” to “10”, which were best fitted by different late-type galaxy templates, namely Sbc, Scd, and Irr (Coleman et al. 1980), and starburst-class templates from SB1 to SB6 (Kinney et al. 1996). Bongiovanni et al. (2019) estimate that the fraction of inaccurate SED fittings for the galaxies contained in the OTELO catalog may amount to up to ~4%. Therefore, our results may be affected if there are ET galaxies miscoded differently from “1” in OTELO, or any of the LT galaxies miscoded as “1”. This could affect, for example, early-type spirals such as Sa galaxies, which are not explicitly included in the OTELO template set. However, the UV SED for ellipticals and S0 galaxies is completely different from Sa and other LT galaxies. The OTELO catalog also includes GALEX-UV data that allow us to identify ET galaxies even in the local universe. Thus, we conclude that recoding the OTELO classification in our galaxy sample as ET and LT classes yields a negligible number of misclassified objects (certainly much less than the OTELO fraction of ~4%) and does not affect our results.

The Sérsic profile is a parametric relationship that expresses the intensity of a galaxy as a function of the distance from its center:

$$I(R) = I_e \exp[-\left(\frac{R/R_e}{b}\right)^n-1],$$

where $I$ is the intensity at a distance $R$ from the galaxy center, $R_e$ is the half-light radius, $I_e$ is the intensity at radius $R_e$, $b$ (~ $2n - 1/3$) is a scale factor, and $n$ is the Sérsic index. Sérsic profiles have been employed for galaxy classification (e.g., Kelvin et al. 2012; Vika et al. 2015). This index provides a geometrical description of the galaxy concentration; for a Sérsic index $n = 4$ we obtain the de Vaucouleurs profile typical of elliptical galaxies, while setting $n = 1$ gives the exponential profile describing spiral galaxies.

Our OTELO Sérsic index and photometry (OTELO SP) sample consists of 1834 galaxies at redshifts $z \leq 2$ extracted from the OTELO catalog (listed under the Z_BEST_deepN code). The sample includes magiz optical photometry from the Canada-France-Hawaii Telescope Legacy Survey3 (CFHTLS), JHKs near-infrared photometry from the WIRCam Deep Survey4 (WIRDS), and Sérsic index estimates obtained using GALAPAGOS2/GALFIT (Häußler et al. 2013; Peng et al. 2002, 2010) on the HST-ACS publicly available data in the F814W band. The sample comprises only galaxies with Sérsic indexes between $n = 0.22$ and $n = 7.9$; Sérsic indexes out of this range are not reliable because of an artificial limit imposed by the Sérsic-profile-fitting algorithm in GALAPAGOS2 (Häußler et al. 2007). Besides, the sample does not include galaxies with Sérsic index values less than three times their estimate errors. For a detailed description of the Sérsic-profile-fitting process we refer to Nadolny et al. (2020).

Figure 1 shows the sample distributions of magnitudes in the $r$ band and photometric redshifts extracted from the OTELO catalog. We note that the sample is not limited in flux, and therefore it is not a complete sample in the volume defined by the redshift limit $z_{\text{phot}} \leq 2$ (see the discussion about magnitude-limited samples below). The redshift distribution presents concentrations at redshifts 0.04, 0.11, 0.34, 0.90, and 1.72 superimposed onto a bell-like distribution with a maximum around $z_{\text{phot}} \approx 0.8$ and a
strong decay from $z_{\text{phot}} \approx 1.3$. The photometric data are incomplete, which affects the available number of galaxies for those classification procedures that cannot effectively manage missing data.

The sample is randomly divided in a training set (70% of the available galaxies) used for the algorithm training, and a test set (30%) used to yield an unbiased estimate of the efficiency of the model. Choosing the proportions of training and test sample sizes depends on a balance between the model performance and the variance in the estimates of the statistical parameters (in our case the accuracy, True ET Rate and True LT Rate, as explained below). Rule-of-thumb proportions often used in machine learning are 90:10 (i.e., 90% training, 10% testing), 80:20 (inspired by the Pareto principle), and 70:30 (our choice). In our case, the 70:30 proportion is justified because it fulfills the large enough sample condition (another rule of thumb) that the sample size must be at least 30 to ensure that the conditions of the central limit theorem are met. Thus, the number of expected ET galaxies in the SP test sample is: $N_{\text{gal}}p_{\text{ET}}p_{\text{est}} \approx 30$, where $N_{\text{gal}} = 1834$ is the sample size, $p_{\text{ET}} = 1834$ is the proportion of ET galaxies in the SP sample, and $p_{\text{est}} = 0.3$ is the proportion of galaxies in the test sample.

2.1.2. Concentration and photometry sample

The concentration is widely used to differentiate ET from LT galaxies. Concentration provides a direct measurement of the intensity distribution in the image of a galaxy. For that reason, the concentration is easier to obtain than the S"ersic index, which requires fitting several parameters to the S"ersic profile.

Here we use the definition (Bershady et al. 2000; Scarlata et al. 2007):

$$C = 5 \log_{10} \left( \frac{r_{80}}{r_{20}} \right),$$

where $r_{80}$ and $r_{20}$ are the 80% and 20% light Petrosian radii, respectively, obtained from the HST F814W band images. We chose the F814W band concentration for compatibility with COSMOS (Scarlata et al. 2007). The data were limited to a redshift $z \leq 2$. The final OTELO concentration and photometry (OTELO CP) sample consists of 2292 galaxies, with 114 classified as ET and 2178 as LT. Figure 2 shows the sample distributions of magnitudes in the $r$ band and photometric redshifts, which is similar to the case of the SP sample discussed above. The CP sample was also divided in two subsamples: a training subsample containing 1604 (70%) of the objects, and a test subsample with 688 (30%) of the galaxies.

2.2. COSMOS samples

We expect that our DNN architecture can be applied to galaxy classification in other databases. Therefore, we checked its reliability using two COSMOS enhanced data products: the Zurich Structure & Morphology Catalog v.1.0 (ZSMC, Scarlata et al. 2007; Sargent et al. 2007) and the COSMOS photometric redshifts v.1.5 (CPhR, Ilbert et al. 2009). Those catalogs have 131 532 and 385 065 entries, respectively. We merged both databases, obtaining 128 442 matches, from which we chose a sample of galaxies with S"ersic index estimates in the range $0.2 < n < 8.8$, and another sample with the same concentration radii used in OTELO. Both samples are limited to redshifts $z < 2$ and include photometry in the CFHT $u$, Subaru $BVgriz$, UKIRT $J$ and CFHT $K$ bands, along with classification entries. Thus, the galaxy records included all the available data from the CPhR bands except the CFHT $i'$ magnitudes (we chose the Subaru $i$ band also included in the catalog).

The resulting COSMOS S"ersic index and photometry (COSMOS SP) sample consists of 34 688 galaxies, 28 951 of which
had been classified as LT and 5737 as ET. With such a large number of galaxies, we can limit the training set to 5000 galaxies (a fraction of approximately 14% of the sample), and rise the fraction of the testing set up to 29 688 galaxies (approximately 86% of the sample) in order to reduce the variance of the results. Analogously, the COSMOS concentration and photometry (COSMOS CP) sample consists of 105 758 galaxies, distributed in 95 781 LT and 9977 ET. We set the corresponding training and testing sets to 10 000 and 95 758 galaxies, respectively.

2.3. Classification procedures

We used a classification baseline and three classification methods for the OTELO samples. The baseline consists in classifying all the galaxies into the most frequent morphological group. Any classification by a more sophisticated method should improve the baseline accuracy. For the COSMOS samples we only used the classification baseline and the DNN architecture developed for the OTELO samples, as we were interested only in probing this architecture.

2.3.1. Color classification

The first classification method uses a color discriminant. After testing several colors, we focus on the $u - r$ color as proposed by Strateva et al. (2001). These authors use a simple color discriminant such that any galaxy with $u - r$ color redder than 2.22 is classified as ET, and LT if $u - r < 2.22$. This method was applied only to both SP and CP samples drawn from OTELO. We also investigated other possible color discriminants that will be presented later. Data records with missing $u - r$ colors were disregarded, reducing the SP sample to 1787 galaxies and the CP sample to 2189.

2.3.2. Linear discriminant analysis

The second classification method is LDA. The aim of LDA is to find a linear combination of features which separates different classes of objects. These features are interpreted as a hyperplane normal to the input feature vectors. We note that the Strateva et al. (2001) $u - r$ color separation method can be regarded as a LDA which defines the $u - r = 2.22$ plane normal to $u - g$ and $g - r$ vectors. As in the previous method, LDA was only applied to SP and CP OTELO samples, and data records with missing $u - r$ colors were disregarded.

Two problems with machine learning techniques are the management of missing data and the curse of dimensionality. Missing data (e.g., a photometric band) usually results in removing objects with incomplete records from the dataset. The curse of dimensionality appears because increasing the number of variables in a classification scheme means that the volume of the space increases very quickly and therefore the data become sparse and difficult to group. The curse of dimensionality can be mitigated by dimensionality reduction techniques such as principal component analysis (PCA), but dimensionality reduction may introduce unwanted effects (data loss, nonlinear relations between variables, and the number of components to be kept Carreira-Perpiñán 2001; Shlens 2014) that tend to blur differences between the groups. Alternative methodologies to deal with these problems are under development, for example by Cai & Zhang (2018) who introduce an adaptive classifier to cope with both missing data and the curse of dimensionality for high-dimensional LDA. To avoid these problems, we chose to limit our LDA model to the Sérsic index and the single highly discriminant $u - r$ color, as it has been already addressed in the galaxy classification literature (e.g., Kelvin et al. 2012; Vika et al. 2015).

2.3.3. Deep neural network

The third method of classification involves a DNN. The sample was analyzed using the Keras library for deep learning. Keras is a high-level neural network application programming interface (API) written in Python under GitHub license. Currently, Keras is available for both Python and R computer languages (Chollet 2017; Chollet & Allaire 2017). In astronomy, Keras has already been used for image classification of galaxy morphologies (Pérez-Carrasco et al. 2019; Domínguez Sánchez et al. 2018) and spectral classification and redshift estimates of quasars (Busca & Ballard 2018), and is included in the astroNN package.

As in the other methods, we use a training and a test set to teach and check the DNN model, respectively. The difference from the other methods is that the structure of their learning discriminant function is predetermined, while the DNN architecture should be tuned on the fly. To achieve this goal, we split the training set in the OTELO samples in (i) a teaching set (80% of the original training set), and (ii) a validation set (the remaining 20%). Compared with OTELO, the COSMOS samples consist of many more galaxies. Therefore, we limited the number of the training sets to 5000 for the COSMOS SP sample, and 10 000 for the CP sample, and conserved the respective teaching set and validation set proportions. We use the teaching set to tune the DNN model, and the validation set to check the loss and accuracy functions that describe the DNN classification capability. Once we have achieved a satisfactory result, the DNN architecture has been optimized to classify the validation set, but the performance may be different for other datasets. To generalize the result, we use the whole original training set to retrain the tuned DNN model, and we then classify the test set galaxies. Therefore, the test set galaxies were used neither to train nor to fine tune the DNN model, but only to evaluate the DNN performance.

An appealing feature of DNNs is the easiness to deal with missing data. In practice, it is enough to substitute the missing values in each normalized variable by zeros to cancel their products on the network weights. The DNN then deals with missing values as if they do not carry any useful information and will ignore them. Of course, it is better if there are not missing values, but DNNs allow the user to treat them without the need of dropping data entries or estimating missing values from other variables.

Baron (2019) provides a succinct description of DNNs, and a complete explanation of Keras elements can be found in Chollet (2017) and Chollet & Allaire (2017). Tuning a DNN is a trial-and-error procedure aimed to find an appropriate architecture and setup. As the numbers of input variables, units, and layers increase, the DNN tends to overfit if the training set is small. For this reason, we kept our DNN model as simple as possible whilst obtaining a high-accuracy classification.

We use standard layers and functions for our model that are already available from Keras. For the interested reader, our DNN architecture consists of two dense layers of 64 units each with rectified linear unit (ReLU) activations, and an output dense layer of a single unit with sigmoid activation. The model was compiled using an iterative gradient descent RMSprop

5 https://astromnn.readthedocs.io/en/latest/
optimizer, a binary-cross-entropy loss function, and accuracy metrics. We kept the default values for the Keras RMSprop optimizer, i.e., a learning rate of 0.001 and a weight parameter for previous batches of $\rho = 0.9$. These values are appropriate for most DNN problems, and moderate changes do not affect the results. We set the number of training epochs to avoid overfitting, and the training batch sizes to appropriate values for the number of records in the DNN training sample in each case.

2.3.4. Bootstrap

We used bootstrap (e.g., Efron & Tibshirani 1993; Chihara & Hesterberg 2018) to obtain reliable statistics that describe the performance of each classification technique. Bootstrapping is a widely used nonparametric methodology for evaluating the distribution of a statistic using random resampling with replacement. Thus, we calculated the classification accuracy and other classification statistics through 100 runs for the $u-r$ color, LDA, and DNN methods. For each run, we also divided the bootstrap random sample in a training set (70%) and a test set (30%).

3. Results

To determine a minimal set of attributes that are able to classify between ET and LT galaxies, we focus on two directly observable characteristics: photometry and shape. Results obtained in previous studies were limited to nearby galaxies. Thus, Strateva et al. (2001) used both the $u$$-$$r$ color and the Sérsic index in the $r$-band to achieve an accuracy of $96.43 \pm 0.04$. Vika et al. (2015) used both the $u$$-$$r$ color and the Sérsic index in the $r$-band to classify a sample of 142 nearby ($z < 0.01$) galaxies, dividing the $u$$-$$r$ versus $n_r$ plane in quadrants; most ET galaxies were located at the $u$$-$$r > 2.3$ and $n_r > 2.5$ quadrant (28 out of 34, i.e., 82% ETs were correctly classified).

3.1. Sérsic index and photometry samples

3.1.1. Baseline classification

The baseline classification is the simplest classification method. It assigns all the samples to the most frequent class. This classification is helpful for determining a baseline performance that is used as a benchmark for other classification methods. For this task, we selected all the galaxies in our OTELO SP sample. In total, there are 1834 galaxy records, 99 of them classified as ET galaxies ($\approx 5.4\%$), and 1735 as LT galaxies ($\approx 94.6\%$). The two groups are unevenly balanced, which results in the baseline classification achieving a high overall accuracy of $94.6\%$, which should be exceeded by any other classification method.

3.1.2. Color classification

A preliminary study was performed to decipher which colors yield a split between ET and LT galaxies that outperforms the baseline. Table 1 shows several examples of the measured accuracy for selecting appropriate single color discriminants. We note that several colors did not perform better than the baseline classification ($94.6\%$), but those involving the $u$ and a red band usually yield the most accurate results. Both $u-J$ and $u-i$ colors perform marginally better than $u-r$, although $u-J$ has a larger number of missing records. We present the rest of the color analysis based on the $u-r$ color in order for ease of direct comparison with the report of Strateva et al. (2001).

Table 2 shows an example of the confusion matrix for a single $u-r$ color bootstrap run, yielding an accuracy of $0.959 \pm 0.009$. Table 3 shows the Accuracy, True ET Rate, and True LT Rate for the different databases and classification methods used in this paper, obtained through the bootstrap procedure. The True ET Rate and True LT Rate both indicate the proportion of ET and LT galaxies, respectively, recovered through the classification procedure. For the $u-r$ color, the statistics yield an average Accuracy of $0.96 \pm 0.02$, a True ET Rate of $0.8 \pm 0.3$, and a True LT Rate of $0.97 \pm 0.02$. The True ET Rate is the least precise of all the statistics in all the samples because of the relatively low number of ET galaxies.

Table 2. One color separation.

<table>
<thead>
<tr>
<th>Color</th>
<th>Accuracy</th>
<th>$N_{\text{test}}$</th>
<th>Separation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u-J$</td>
<td>$0.96 \pm 0.01$</td>
<td>518</td>
<td>4.1 $\pm$ 0.2</td>
</tr>
<tr>
<td>$u-i$</td>
<td>$0.96 \pm 0.01$</td>
<td>536</td>
<td>2.8 $\pm$ 0.3</td>
</tr>
<tr>
<td>$u-r$</td>
<td>$0.96 \pm 0.02$</td>
<td>536</td>
<td>2.0 $\pm$ 0.2</td>
</tr>
<tr>
<td>$u-H$</td>
<td>$0.95 \pm 0.01$</td>
<td>510</td>
<td>Baseline</td>
</tr>
<tr>
<td>$g-J$</td>
<td>$0.94 \pm 0.02$</td>
<td>527</td>
<td>Baseline</td>
</tr>
<tr>
<td>$g-i$</td>
<td>$0.94 \pm 0.01$</td>
<td>548</td>
<td>Baseline</td>
</tr>
</tbody>
</table>

Notes. Column 1: tested color. Column 2: mean accuracy (proportion of galaxies correctly classified) on 100 random test sets; we note that the colors are sorted from the highest to the lowest accuracy score. Column 3: sample size included in each test set; differences in the sample size between different colors are due to missing data. Column 4: color discriminant value or Baseline if the accuracy score is not statistically different from the baseline classification.

Table 2. Color $u-r$ confusion matrix.

<table>
<thead>
<tr>
<th>Color</th>
<th>ET</th>
<th>LT</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>OTELO</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ET</td>
<td>25</td>
<td>489</td>
<td>514</td>
</tr>
<tr>
<td>LT</td>
<td>25</td>
<td>489</td>
<td>514</td>
</tr>
<tr>
<td>Total</td>
<td>27</td>
<td>509</td>
<td>536</td>
</tr>
</tbody>
</table>

A134, page 6 of 15
Table 3. Comparison of classification methods for SP samples.

<table>
<thead>
<tr>
<th>Database</th>
<th>Method</th>
<th>Accuracy (^{(a)})</th>
<th>True ET Rate (^{(a)})</th>
<th>True LT Rate (^{(a)})</th>
<th>Sample size</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Mean</td>
<td>Error</td>
<td>Mean</td>
<td>Error</td>
</tr>
<tr>
<td>OTELO</td>
<td>Baseline</td>
<td>0.946</td>
<td>0.006</td>
<td>0</td>
<td>...</td>
</tr>
<tr>
<td>OTELO</td>
<td>(u - r) color</td>
<td>0.96</td>
<td>0.02</td>
<td>0.8</td>
<td>0.3</td>
</tr>
<tr>
<td>OTELO</td>
<td>LDA</td>
<td>0.970</td>
<td>0.008</td>
<td>0.80</td>
<td>0.08</td>
</tr>
<tr>
<td>OTELO</td>
<td>DNN</td>
<td>0.985</td>
<td>0.007</td>
<td>0.84</td>
<td>0.09</td>
</tr>
<tr>
<td>COSMOS</td>
<td>Baseline</td>
<td>0.835</td>
<td>0.002</td>
<td>0</td>
<td>...</td>
</tr>
<tr>
<td>COSMOS</td>
<td>DNN</td>
<td>0.967</td>
<td>0.002</td>
<td>0.91</td>
<td>0.03</td>
</tr>
</tbody>
</table>

Notes. \(^{(a)}\)On 100 bootstrap runs.

Fig. 3. Classification for the OTELO SP sample of 1834 galaxies through the \(u - r\) color and LDA algorithms. The \(u - r\) color vs. logarithm of the Sérsic index \(n\) plot shows the original morphological type classification in the OTELO catalog reduced to LT galaxies (black circles) and ET galaxies (red squares). The dotted blue line indicates the \(u - r\) color separation, and the dashed green line the LDA separation by the \(u - r\) color and the Sérsic index. The logarithmic scale for the Sérsic index makes the comparison with the concentration in Fig. 10 (which is already a logarithmic quantity) easier, but it bends the LDA line. The reader should take into account that this is not a flux limited sample.

Fig. 4. Comparative distribution of the \(u - r\) color and redshifts for the 1834 galaxies in the OTELO SP sample. Bottom left panel: \(u - r\) color vs. photometric redshift \(z_{\text{phot}}\) plot shows the original morphological type classification in the OTELO catalog reduced to LT galaxies (black circles) and ET galaxies (red squares). The dotted blue line indicates the \(u - r\) color separation. Top panel: SP sample photometric redshift distribution. Right panel: SP sample \(u - r\) color distribution.

extreme bootstrap runs with accuracies lying in the 0.915–0.92 interval fail to detect any ET galaxy.

The True ET Rate and True LT Rate are analogous to the true positive rate and false positive rate \(\left(=\text{1} - \text{True LT Rate}\right)\) statistics. These statistics are used in receiver operating characteristic (ROC) curves to represent the ability to discriminate between two groups as a function of a variable threshold, usually the likelihood of the classification (e.g., Baron 2019). Figure 6 shows the distribution of bootstrap values in the True ET Rate versus True LT Rate plane. Every point in this figure corresponds to the 50% probability threshold of the ROC curve (not shown) for each bootstrap run. The closer the point to the top-right corner, the better the classification. The data point located at True LT Rate = 1, True ET Rate = 0 corresponds to the two \(u - r\) color bootstrap runs that failed to detect any ET galaxy. Below, for the LDA and DNN classification methods, we increase the number of predictor variables used to enhance the distinction between ET and LT galaxies.

3.1.3. Linear discriminant analysis classification

Although the use of colors is an improvement on the baseline classification, and the \(u - r\) plane method is very easy to implement, we dispose of additional data in order to aim for more powerful classification techniques. In particular, it will be very helpful to include a parameter associated with the galaxy morphology that can be inferred from optical or near-infrared observations. The Sérsic profile in Eq. (1) describes the intensity of a galaxy as a function of the distance from its center regardless of the galaxy colors, and thus can be useful for our purpose.

The dataset combining \(u - r\) colors and Sérsic indexes has been plotted using linear discriminant analysis. The sample with complete records consisted of 1787 galaxies which have been split in a training group of 1251 and a test group of 536. Figure 3 shows the LDA separation in the \(u - r\) color versus Sérsic index \(n\) plane for the test galaxies. The logarithmic scale for the
Sérsic index axis makes the visual comparison with the concentration index (which is already a logarithmic quantity) easier, but at the cost of showing a bent LDA line. The $u-r$ color is the main discriminant, but the Sérsic index helps to separate the ET and LT sets more clearly. The separation line is located at $u-r = (2.756 \pm 0.002) - (0.14125 \pm 0.00007)n$, where $n$ is the Sérsic index. An example for the confusion matrix for the test set LDA classification is shown in Table 4. For a total of 536 test galaxies, only 15 ($7 + 8$) were misclassified, yielding a classification accuracy of $0.972 \pm 0.008$ in this particular case.

Linear discriminant analysis improves both the baseline and the $u-r$ color classifications, as shown in Table 3 and Fig. 5. The average True ET Rate of 0.80 is similar to the $u-r$ color, and the True LT Rate of 0.979 is marginally larger. Altogether, including the Sérsic index has helped to obtain a moderate improvement on the average accuracy (from 0.96 to 0.970) but reduces the accuracy uncertainty by 60% (from 0.02 to 0.008) with respect to the $u-r$ color discriminant.

The LDA classification presented above is a simple machine learning methodology that shows the potential of this kind of algorithm. As with most machine learning methods, LDA does not incorporate an easy solution to deal with missing data, although the research in this area has been continuous over the last 50 years (e.g., Jackson 1968; Chan et al. 1976; Cai & Zhang 2018). Therefore, the usual way to deal with missing values is simply dropping incomplete records. This is a major problem when dealing with cross-correlated data gathered from multiple catalogs because missing data is a frequent characteristic of catalog entries. Thus, to prevent a drastic reduction in the amount of complete records, we are forced to put a limit on the number of photometric colors.

Table 4. LDA confusion matrix.

<table>
<thead>
<tr>
<th></th>
<th>OTELO</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ET</td>
<td>LT</td>
</tr>
<tr>
<td>LDA</td>
<td>20</td>
<td>8</td>
</tr>
<tr>
<td>LT</td>
<td>7</td>
<td>501</td>
</tr>
<tr>
<td>Total</td>
<td>27</td>
<td>509</td>
</tr>
</tbody>
</table>

Table 5. OTELO DNN confusion matrix.

<table>
<thead>
<tr>
<th></th>
<th>OTELO</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ET</td>
<td>LT</td>
</tr>
<tr>
<td>DNN</td>
<td>27</td>
<td>4</td>
</tr>
<tr>
<td>LT</td>
<td>4</td>
<td>516</td>
</tr>
<tr>
<td>Total</td>
<td>31</td>
<td>520</td>
</tr>
</tbody>
</table>

3.1.4. DNN classification

Classification based on DNNs allows us to overcome the missing data problem that limits the number of feasible variables of other machine learning solutions. This feature by itself justifies its application in astronomical databases, where records are often incomplete. In the following, we show the results obtained for both OTELO and COSMOS photometry and Sérsic index samples.

OTELO. We applied a very simple DNN to the OTELO catalog. First we computed the colors $u-r, u-g, r-i, r-z, r-J, r-H$, and $r-K_s$, and we introduced these colors as inputs in the DNN along with the $r$ magnitude and the Sérsic index, that is, a total of nine input factors feeding the DNN. One example of the 100 random samplings analyzed with our DNN classification is shown in Table 5. For this particular example, the classification accuracy is $0.985 \pm 0.006$. We highlight the fact that, because of the missing data management, the number of cases included in the DNN classification (551) is larger than those for the $u-r$ color.
Table 6. OTELO DNN mismatches.

<table>
<thead>
<tr>
<th>ID</th>
<th>OTELO</th>
<th>DNN</th>
<th>Prob.</th>
<th>$z_{phot}$</th>
<th>$n$</th>
<th>C</th>
<th>Elong.</th>
<th>Size (px$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>267</td>
<td>LT</td>
<td>ET r</td>
<td>0.32</td>
<td>0.77</td>
<td>1.59</td>
<td>3.55</td>
<td>1.88</td>
<td>259</td>
</tr>
<tr>
<td>496</td>
<td>LT</td>
<td>ET v</td>
<td>0.12</td>
<td>0.70</td>
<td>2.54</td>
<td>3.54</td>
<td>1.22</td>
<td>231</td>
</tr>
<tr>
<td>1895</td>
<td>ET</td>
<td>LT r</td>
<td>1.00</td>
<td>0.04</td>
<td>0.72</td>
<td>3.47</td>
<td>1.22</td>
<td>61</td>
</tr>
<tr>
<td>2818</td>
<td>LT</td>
<td>ET v</td>
<td>0.12</td>
<td>0.72</td>
<td>3.29</td>
<td>3.32</td>
<td>1.39</td>
<td>255</td>
</tr>
<tr>
<td>3680</td>
<td>ET</td>
<td>LT v</td>
<td>1.00</td>
<td>1.45</td>
<td>0.36</td>
<td>2.14</td>
<td>1.49</td>
<td>27</td>
</tr>
<tr>
<td>4010</td>
<td>LT</td>
<td>ET v</td>
<td>0.08</td>
<td>0.33</td>
<td>3.91</td>
<td>4.29</td>
<td>1.09</td>
<td>1002</td>
</tr>
<tr>
<td>4923</td>
<td>ET</td>
<td>LT v</td>
<td>1.00</td>
<td>0.08</td>
<td>0.41</td>
<td>1.12</td>
<td>1.04</td>
<td>55</td>
</tr>
<tr>
<td>10207</td>
<td>ET</td>
<td>LTv</td>
<td>1.00</td>
<td>0.12</td>
<td>1.62</td>
<td>2.31</td>
<td>1.99</td>
<td>21</td>
</tr>
</tbody>
</table>

Notes. Column 1: galaxy identifier in the OTELO catalog. Column 2: OTELO classification. Column 3: DNN classification and a letter code to indicate reject (r) or validate (v); this classification after visual inspection by three of the authors. Column 4: DNN classification likelihood, closer to zero for ET instances and closer to one for LT. Columns 5–7: the photometric redshift, the Sérsic index, and the concentration value, respectively. Column 8: shows the elongation, that is, the ratio between the major and minor axes of the galaxy image as calculated by SExtractor (Bertin & Arnouts 1996). Column 9: shows the area in pixels of the HST Advanced Camera for surveys (scale 0.03 arcsec px$^{-1}$).

Fig. 7. OTELO – DNN discrepancies. Relative declination vs. right ascension coordinates in arcsec. First column: combined HST images from the F814W (reddish) and F606W (greenish) bands, with galaxy ID at the top-right corner. Second column: GALFIT models for the light distribution. Third column: HST minus GALFIT model residuals. Columns fourth, fifth and sixth: repeat the order of the previous columns.

and LDA methods (536), despite the differences in the number of input factors (9 for the DNN versus 2 for the LDA or 1 for the $u – r$ color) which in most machine learning techniques would lead to a larger number of incomplete records being left out.

The mean accuracy for our 100 DNN samplings is 0.985 ± 0.007, as shown in Table 3 and in Fig. 5. The True ET Rate is 0.84, marginally larger than the $u – r$ and LDA values, and the True LT Rate is the highest of the three methods tested.

Table 6 shows the eight discrepancies between the DNN and OTELO classifications for the test sample data set presented in Table 5.

Figure 7 presents the HST images in the F814W band for these eight galaxies. For the visual classification, we have taken into account the galaxy elongation and the light distribution in the HST image; the GALFIT model helps to indicate the shape and orientation, and the image residuals indicate a possible lack
of fitting or possible substructures not visible in the HST image. Elongated and fuzzy images support a LT visual classification, while a round and soft appearance points to an ET galaxy. From our visual check, we conclude that six out of the eight galaxies with different class ascertainment are correctly classified by our DNN algorithm. Following is a brief description of each mismatched object.

- ID 267. A north–south oriented disk galaxy with a fuzzy northeast portion. The bulge of the galaxy broadly dominates the disk component. Compatible with a Sab class. Visual classification as LT.
- ID 496. A rounded smooth galaxy with a visual LT companion at the northwest and a star at the southwest. Visual classification as ET.
- ID 1895. Appears as a rounded and compact galaxy in the HST F814W image (our detection image used for GALAPAGOS). However, visual inspection of the HST F606W image shown in Fig. 8 reveals that there is a companion source not detected in F814W. Using our web-based graphic user interface we find that this companion, probably a LT galaxy neither detected in the OTELO deep image, enters the ellipse which was used to extract photometry. It is likely that a composite SED could be well fitted by LT templates instead single-population ones. Visual classification as ET with an unresolved companion.
- ID 2818. A round shaped galaxy, the image of residuals suggests possible over-subtraction. Visual classification as ET.
- ID 3680. A small, fuzzy, northwest to southeast oriented disk galaxy. Visual classification as LT.
- ID 4010. A rounded galaxy, with a LT companion at the southeast. Visual classification as ET.
- ID 4923. A faint and fuzzy galaxy. Visual classification as LT.
- ID 10207. A west-east oriented fuzzy small disk galaxy. Visual classification as LT.
- ID 2670. A north–south oriented fuzzy small disk galaxy. Visual classification as LT.

**COSMOS.** We used the COSMOS dataset to check for the reliability of our DNN architecture. Using the ZSMC and CPhR catalogs we built a sample of 34 688 galaxies for which the photometry and Sérsic indexes are available. Photometric bands in the CPhR catalog do not exactly match OTELO’s bands. We have included Subaru’s BV bands, and have excluded the H band which is absent from the CPhR database. Thus, the COSMOS data used in this work consist of nine photometric bands (compared with eight in the case of OTELO catalog) and the Sérsic index. Because the OTELO and COSMOS bands are different, we had to train our DNN model again. As in the case of OTELO, we fed the DNN with the Sérsic index, the r magnitudes, and the colors relative to the r band. We did so without changing the DNN architecture except for the number of inputs. Despite the differences between the two datasets, we shall see that our DNN architecture reaches a high classification accuracy also for the COSMOS data.

Table 7 shows the confusion matrix for one of the 100 random samplings that we used to characterize the COSMOS DNN. For this sampling in particular, the classification accuracy is of 0.967 ± 0.001. Figure 9 and Table 3 show the distribution of accuracies for 100 DNN classification trials obtained from the COSMOS dataset. The mean accuracy for these trials is 0.967 ± 0.002, well above the relatively low baseline of 0.835 ± 0.002, which corresponds to 28 951 LT galaxies out of a total of 34 688 objects included in our COSMOS SP sample. Not only is the COSMOS SP baseline lower than OTELO’s (0.946), but the DNN

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The Sérsic index that we used in the LDA and DNN classification methods detailed above is obtained through a parametric fitting that is difficult to achieve when dealing with low-resolution images. On the contrary, the radius containing a given fraction of the galaxy total brightness is easier to estimate and can be measured directly. In this section we repeat our previous analysis of the OTELO and COSMOS databases, but using samples obtained through the concentration index defined as the ratio between the radii containing 80% and 20% of the galaxy brightness.

Table 8 shows the results obtained with the OTELO and COSMOS CP samples. As in the Sérsic index samples, the DNN classification yields the highest accuracy for OTELO (0.980), and also yields very accurate results for COSMOS (0.971). In general, the results are comparable with those obtained using the SP sample.

Figure 10 shows the distribution of the $u - r$ colors versus the concentration index, along with the $u - r$ color and the LDA separation boundaries. The $u - r$ color separation is $2.1 \pm 0.3$, in agreement with the values for the OTELO SP sample ($2.0 \pm 0.2$), and Strateva et al. (2001, $u - r = 2.22$). The LDA separation is located at

$$u - r = (3.882 \pm 0.002) - (0.5342 \pm 0.0003)C,$$

where $C$ is the concentration. The same trend of LT galaxies getting bluer at redshifts $z > 0.5$ can be seen in Fig. 11.

3.3. Magnitude limited samples

Our aim in this paper is to use machine learning techniques to distinguish between ET and LT galaxies. Thus, our samples are selected from a redshift limited region with the only requirement of containing enough galaxies in every redshift interval for accurate training and testing the machine learning algorithm.
However, neither OTELO nor COSMOS SP and CP samples were flux limited to produce a complete sample of galaxies in the volume defined by $z \leq 2$. This leads us to question the possible cosmological inferences of our results.

In this section, we present the results of the machine learning algorithms but using flux limited samples for both training and testing sets. Figure 14 shows the cumulative distribution of galaxies by $r$ magnitudes for all the samples analyzed so far. With respect to the low-brightness tails, both OTELO SP and CP samples have similar cumulative distributions that flatten around a magnitude of $r \approx 26$. This flattening may be considered as a rough measurement of completeness. Thus, compared with OTELO-Deep image measurements, Bongiovanni et al. (2019) estimate that the OTELO catalog reaches a 50% completeness flux at magnitude 26.38. For COSMOS, the SP sample flattens around $r \approx 23$, while the CP sample does at $r \approx 24$. Since COSMOS samples cover a large sky volume, their high brightness tails extend to galaxies approximately 1.5 magnitudes brighter than the much more confined OTELO volume.

We check our machine learning algorithms using flux-limited samples. Table 9 shows the results of 100 bootstrap runs on different OTELO $r$-magnitude-limited samples. We highlight the fact that all the $u - r$ color, LDA, and DNN accuracies are

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**Fig. 11.** As Fig. 4 but for the 2292 galaxies in the OTELO CP sample.

**Fig. 12.** As Fig. 5 but for the 100 galaxy classification bootstrap runs for the 2292 galaxies of the OTELO CP sample.

**Fig. 13.** Histogram of accuracies for 100 galaxy classification bootstrap runs using the COSMOS CP sample. The solid black line corresponds to the baseline accuracy distribution of a sample of 105 758 COSMOS galaxies. The blue histogram and dash-dotted line shows the DNN accuracy distribution for a test sample of 95 758 galaxies.

**Fig. 14.** Cumulative distribution of galaxies by $r$ magnitudes. OTELO SP and CP samples are 3 and 2 magnitudes deeper than the COSMOS SP and CP samples, respectively. However, COSMOS sweeps a larger volume as the brightest end of the cumulative distribution implies.
consistent within the errors. However, for brighter samples, we can observe a downward trend in accuracies and upward trend in uncertainties for the LDA and DNN classifications, while the $u-r$ color results remain basically without change. Analogously, Table 10 shows the limit $r$ magnitude (Col. 1), the Sérsic index (Col. 2), and the Baseline DNN accuracy for the COSMOS SP and CP samples. In this case, the training set size is always 5000 for the SP and 10,000 for the CP samples, except for the CP limit magnitude $r \leq 22$ with a sample size of 9852, for which the training set was set to 5000. As in the OTELO case, we notice the consistency of the DNN accuracies within the errors, and the trend towards lower accuracies and larger uncertainties.

There are two effects that may account for the trends in accuracy and uncertainty observed in the LDA and DNN classification methods. On one hand we detect a tendency for a lower proportion of LT galaxies in brighter galaxies, indicated by the baseline decrease. As the a priori probabilities of a galaxy to be ET or LT are more alike, the uncertainty in the classification increases. On the other hand, as the sample size shrinks in brighter samples, so do the fractions of the sample reserved for training and testing (70% and 30%, respectively). This shrinking of the sample size leads to a less satisfactory training and a less precise testing. Both effects, the baseline decrease and the sample shrinking, tend to reduce the classification accuracy. With respect to the $u-r$ classification, the $u-r$ color discriminant is determined by low-redshift galaxies (see Figs. 4 and 11) that tend to dominate flux limited samples. Thus, the discriminant remains constrained around a value of 2, and the classification accuracy remains around 0.96. For the brighter SP and CP samples, with magnitude limit $r \leq 25$, the LDA and the DNN accuracies are similar to that of the $u-r$ color. In the other two magnitude-limited cases ($r \leq 26$ and $r \leq 27$), the DNN presents the highest accuracy, and the accuracy of the LDA is higher than the $u-r$ color. These results show that all the machine learning methods for classification presented in this paper are robust for both limited and unlimited flux samples.

### 4. Conclusions

Neural networks are becoming increasingly important for image classification and will play a fundamental role in mining future databases. However, many of the current astronomical databases consist of catalogs of tabulated data. Machine learning techniques are often used to analyze astronomical tabulated data, but analysis through DNNs is far less frequent and limited to low-redshift galaxies.

Here, we provide a consistent and homogeneous comparison of the popular techniques used in the literature for binary ET and LT morphological type classification of galaxies up to redshift $z \leq 2$. We used data from the OTELO catalog for classifying galaxies by means of (i) the single $u-r$ color discriminant, (ii) LDA using $u-r$ color and the shape parameter (Sérsic or concentration index), and (iii) DNN fed by visual-to-NIR photometry and shape parameter. We also applied the DNN architecture developed for OTELO on COSMOS to probe its reliability and reproducibility in a different database.

Both Sérsic index and concentration index shape parameters yield comparable results, but using the concentrations allowed to increase the size of OTELO and COSMOS available data. All the machine learning methodologies for galaxy classification tested in this paper are robust and produce comparable results for both limited and unlimited flux samples. Accuracy, True ET Rate, and True LT Rate estimates show that DNN outperforms the other two methods and allows the user to classify more objects because of the missing data management.

These results show that DNN classification is a powerful and reliable technique to mine existing optical astronomical databases. For unresolved objects, the morphological identification is unattainable, the spectrum of a dim object is very difficult to obtain, and multiwavelength data are usually unavailable. For
most objects, photometric visible and near infrared observations are the only (and usually incomplete) accessible data.

This study indicates that DNN classification may address the mining of currently available astronomical databases better than other popular techniques.

An important limitation for all machine learning techniques is the availability of labeled data, that is, data that have already been classified or measured. This limited us to a binary ET and LT classification and to impose a redshift threshold. Incorporating reliable synthetic data for classification training is an important goal if we wish to overcome these limitations.

Our results provide compelling support for extending the DNN classification to targets other than binary morphological classification of galaxies, such as separating stars from galaxies, deciphering the spectral type of stars, and detecting rare events. The application of DNN is not restricted to classification problems. Our results strongly suggest that DNN methods can also be very effective in exploring other issues such as, for example, photometric redshift estimates.

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