

J^{--} Glueballs and a Low Odderon Intercept

Felipe J. Llanes-Estrada,¹ Pedro Bicudo,² and Stephen R. Cotanch³

¹*Departamento de Física Teórica I, Universidad Complutense de Madrid, 28040 Madrid, Spain*

²*Departamento de Física and CFIF, Instituto Superior Tecnico, Av. Rovisco Pais, 1049-001 Lisboa, Portugal*

³*Department of Physics, North Carolina State University, Raleigh, North Carolina 27695-8202, USA*

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We report an odderon Regge trajectory emerging from a field theoretical Coulomb gauge QCD model for the odd signature J^{PC} ($P = C = -1$) glueball states. The trajectory intercept is clearly smaller than the Pomeron and even the ω trajectory's intercept which provides an explanation for the nonobservation of the odderon in high energy scattering data. To further support this result we compare to glueball lattice data and also perform calculations with an alternative model based upon an exact Hamiltonian diagonalization for three constituent gluons.

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Regge trajectories [1] have long been an effective phenomenological tool in hadronic physics. In Regge theory the scattering amplitude is governed by Regge poles, $\alpha_n(s)$, in the complex J (angular momentum) plane. For integer J the amplitude has a pole in the complex s plane and, by crossing symmetry, for $t < 0$ at high s the cross section is dominated by the Regge trajectory, $\alpha(t) = bt + \alpha(0)$, with the largest intercept, $\alpha(0)$. This conjecture provides a unifying connection between hadron spectroscopy (Chew-Frautschi plot of J versus $t = M_J^2$) and the high energy behavior of the total cross section which scales as $s^{\alpha(0)-1}$. For elastic scattering the energy dependence is well described by the leading Regge trajectory, the Pomeron, having $\alpha_P(0) \cong 1$ and $b_P = 0.2-0.3 \text{ GeV}^{-2}$ [for recent fits see Ref. [2]]. Of course the Pomeron does not relate to conventional hadron spectra since meson trajectories typically have larger slopes, $b_M \cong 0.9 \text{ GeV}^{-2}$, and smaller intercepts, $\alpha_M(0) \cong 0.55$. According to the glueball-Pomeron conjecture [3,4], supported by lattice [5] and other models [6], this trajectory is instead connected to glueball spectroscopy. The different Pomeron and meson trajectory slopes can be generated [4] by the gg and $q\bar{q}$ color factors, respectively, used in confining 2-body models. Because of the large gluon mass gap, which suppresses relativistic corrections and transverse gluon exchange [7], these models tend to be more robust for glueballs than mesons. They produce a Pomeron consisting of even signature J^{++} glueballs having maximum intrinsic spin S coupled to minimum possible orbital L .

Of active interest is the odd signature, $P = C = -1$ counterpart to the Pomeron, the odderon [8], for which there is no firm experimental evidence. Whereas the Pomeron predicts asymptotically equal pp and $\bar{p}p$ cross sections, the competitive presence of the odderon or any other $C = -1$ trajectory would produce a difference. However, high energy measurements reveal a minimal difference indicating that the odderon, if it exists, would have a smaller intercept probably at most comparable to the ω value, $\alpha_\omega(0) = 0.5$. Indeed, dedicated exclusive searches at HERA [9] exclude an odderon Regge trajectory

with an intercept greater than 0.7. Although perturbative QCD calculations [10] based on the BKP equation predict an odderon intercept close to 1, they are only reliable for both $s, -t \gg \Lambda_{\text{QCD}}$ and thus suspect for $\alpha(t=0)$. For example, the predicted Pomeron intercept using the similar BFKL equation is 1.5 in conflict with data.

In this Letter we summarize recent nonperturbative QCD calculations based on lattice gauge theory and QCD models incorporating fundamental elements which produce realistic hadron spectra with Regge trajectories. Our key results clarify and dispel several misconceptions concerning the odderon. First, we document an odderon trajectory of odd signature J^{--} glueballs [that we call *oddballs*, a name first used for exotic mesons [11] and subsequently exotic glueballs [12]]. Its intercept is well below 0.7, consistent with experimental searches. Second, the odderon and Pomeron have similar slopes, in analogy with the similar-slope meson (two-body) and baryon (three-body) Regge trajectories. Third, the lightest resonance on the odderon is the 3^{--} , not the 1^{--} which is on a daughter trajectory. In the framework of constituent models, the odderon begins with a 3^{--} three-gluon $L = 0$ state with maximum spin S , similar to the two-gluon Pomeron beginning with the s wave, spin aligned 2^{++} glueball. Higher odd signature states on the odderon have the same S but increasing L (e.g., $d, g \dots$ waves producing $J^{PC} = 5^{--}, 7^{--} \dots$).

The first constituent three-gluon calculations [13,14] utilized a nonrelativistic potential model. They reported [14] the nearly degenerate lightest states, $J^{PC} = 0^{-+}, 1^{--}$, and 3^{--} , with masses about 4.8 times the constituent gluon mass. Hyperfine splittings breaking this degeneracy were considered in the bag model [15] but the global mass scale was too low [3]. Another problem confronting early models was a spurious two-gluon $J = 1$ state (unlike photons, constituent gluons have 3 spin projections) which violates boson statistics (Yang's theorem). This issue is naturally resolved in the Coulomb gauge effective QCD formulation [16] in which the Fock operator commutation relations permit only transverse gluons respecting Yang's theorem.

The connection between constituent gluons and QCD via a dynamical mass generation mechanism is well documented [17,18].

Our calculation is based on this relativistic many-body Hamiltonian formulation which unifies the quark and glue sectors. This approach dynamically generates constituent gluon and quark masses [while respecting chiral symmetry [19,20]], produces reasonable quark and gluon condensates, describes flavored meson spectra, including hyperfine splittings [21], and predicts exotic hybrids [22] and $C = +1$ glueballs [4,16] consistent with lattice gauge results. Also noteworthy, this formulation entails only two dynamical parameters (same for both quark and glue sectors). Consult Refs. [20,21,23] for further details.

The effective QCD Hamiltonian in the gluon sector is

$$H_{\text{eff}}^g = \text{Tr} \int d\mathbf{x} [\mathbf{\Pi}^a(\mathbf{x}) \cdot \mathbf{\Pi}^a(\mathbf{x}) + \mathbf{B}_A^a(\mathbf{x}) \cdot \mathbf{B}_A^a(\mathbf{x})] - \frac{1}{2} \int d\mathbf{x} d\mathbf{y} \rho_g^a(\mathbf{x}) V(\mathbf{x}, \mathbf{y}) \rho_g^a(\mathbf{y}), \quad (1)$$

with color charge density $\rho_g^a(\mathbf{x}) = f^{abc} \mathbf{A}^b(\mathbf{x}) \cdot \mathbf{\Pi}^c(\mathbf{x})$, gauge fields \mathbf{A}^a , conjugate momenta $\mathbf{\Pi}^a = -\mathbf{E}^a$, and Abelian components $\mathbf{B}_A^a = \nabla \times \mathbf{A}^a$, for $a = 1, 2, \dots, 8$. The normal mode expansions are

$$\mathbf{A}^a(\mathbf{x}) = \int \frac{d\mathbf{q}}{(2\pi)^3} \frac{1}{\sqrt{2\omega_k}} [\mathbf{a}^a(\mathbf{q}) + \mathbf{a}^{a\dagger}(-\mathbf{q})] e^{i\mathbf{q} \cdot \mathbf{x}}, \quad (2)$$

$$\mathbf{\Pi}^a(\mathbf{x}) = -i \int \frac{d\mathbf{q}}{(2\pi)^3} \sqrt{\frac{\omega_k}{2}} [\mathbf{a}^a(\mathbf{q}) - \mathbf{a}^{a\dagger}(-\mathbf{q})] e^{i\mathbf{q} \cdot \mathbf{x}}, \quad (3)$$

with the Coulomb gauge transverse condition, $\mathbf{q} \cdot \mathbf{a}^a(\mathbf{q}) = (-1)^\mu q_\mu a_{-\mu}^a(\mathbf{q}) = 0$. Here $a_\mu^a(\mathbf{q})$ ($\mu = 0, \pm 1$) are the bare gluon Fock operators from which, by a Bogoliubov-Valatin canonical transformation, the dressed gluon or quasiparticle operators, $\alpha_\mu^a(\mathbf{q}) = \cosh\Theta(q) a_\mu^a(\mathbf{q}) + \sinh\Theta(q) a_\mu^{a\dagger}(-\mathbf{q})$, emerge. This similarity transformation is a hyperbolic rotation similar to the BCS fermion treatment. These operators excite constituent gluon quasiparticles from the BCS vacuum, $|\Omega\rangle_{\text{BCS}}$, and satisfy the transverse commutation relations, $[\alpha_\mu^a(\mathbf{q}), \alpha_\nu^{b\dagger}(\mathbf{q}')] = \delta_{ab} (2\pi)^3 \delta^3(\mathbf{q} - \mathbf{q}') D_{\mu\nu}(\mathbf{q})$, with $D_{\mu\nu}(\mathbf{q}) = [\delta_{\mu\nu} - (-1)^\mu \frac{q_\mu q_\nu}{q^2}]$. Finally, the quasiparticle or gluon self-energy, $\omega(q) = q e^{-2\Theta(q)}$, satisfies a gap equation [16]. Both confinement and the leading QCD canonical interaction are contained in the Cornell type potential $V = \sigma r - \frac{\alpha_s}{r}$ with string tension, $\sigma = 0.18 \text{ GeV}^2$, determined by lattice gauge calculations and $\alpha_s = 0.42$. For this interaction the calculated gluon constituent mass from the gap equation, which uses the cutoff or renormalization parameter $\Lambda = 1.1 \text{ GeV}$, is $m_g \equiv \omega(0) \cong 0.8 \text{ GeV}$. Previous two constituent applications ($q\bar{q}$ mesons and gg glueballs) involved Tamm-Dancoff (TDA) and random phase approximation (RPA) Hamiltonian diagonalizations whereas three-body ($q\bar{q}g$ hybrids) predictions utilized a variational calculation which was found to be accurate when tested in

two-body systems. We therefore adopt the variational method for predicting the ggg oddballs which is the minimum Fock space assignment for $C = -1$ glueballs. The three-gluon variational wave function is

$$|\Psi^{\text{JPC}}\rangle = \int d\mathbf{q}_1 d\mathbf{q}_2 d\mathbf{q}_3 \delta(\mathbf{q}_1 + \mathbf{q}_2 + \mathbf{q}_3) F_{\mu_1\mu_2\mu_3}^{\text{JPC}}(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) \times C^{abc} \alpha_{\mu_1}^{a\dagger}(\mathbf{q}_1) \alpha_{\mu_2}^{b\dagger}(\mathbf{q}_2) \alpha_{\mu_3}^{c\dagger}(\mathbf{q}_3) |\Omega\rangle_{\text{BCS}}, \quad (4)$$

with summation over repeated indices. The color tensor C^{abc} is either totally antisymmetric f^{abc} (for $C = 1$) or symmetric d^{abc} (for $C = -1$). Boson statistics thus requires the $C = -1$ oddballs to have a symmetric space-spin wave function taken here to have form

$$F_{\mu_1\mu_2\mu_3}^{\text{JPC}}(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) = [c_{12} f(q_1, q_2) + c_{23} f(q_2, q_3) + c_{13} f(q_1, q_3)] [Y_L^\lambda(\hat{\mathbf{q}}_1) + Y_L^\lambda(\hat{\mathbf{q}}_2) + Y_L^\lambda(\hat{\mathbf{q}}_3)], \quad (5)$$

$$c_{12} = \langle 1\mu_1 1\mu_2 | s\mu_s \rangle \langle s\mu_s 1\mu_3 | S\mu \rangle \langle L\lambda S\mu | J\mathcal{M} \rangle, \quad (6)$$

appropriate for this analysis of the lightest states which are either s or d wave oddballs with a single L excitation. The other two coefficients in Eq. (5) can be obtained by permuting the indices in Eq. (6). A more comprehensive treatment would include other orbital angular (or radial) excitations but since these are considerably separated in energy (more so than for conventional meson states) this mixing is small. Several forms for the variational radial wave function, $f(q, q')$, involving two variational parameters, β and β' , were investigated including a separable form, $f(q)f(q')$, which only involves one parameter. From previous experience [22], reliable, accurate variational solutions can be obtained if these functions have a bell-shaped form with scalable variational parameters. In particular, we found numerical solutions of the ρ meson TDA problem for the same potential to be especially accurate.

The variational equation for the J^{PC} glueball with mass M_{JPC} is

$$\frac{\langle \Psi^{\text{JPC}} | H_{\text{eff}}^g | \Psi^{\text{JPC}} \rangle}{\langle \Psi^{\text{JPC}} | \Psi^{\text{JPC}} \rangle} = M_{\text{JPC}}. \quad (7)$$

For clarity and insight it is worthwhile to express $H_{\text{eff}}^g = H_{\text{se}} + H_{\text{sc}} + H_{\text{an}}$ as a sum of three terms corresponding to self-energy (two-body contributions), H_{se} , scattering (instantaneous exchange interaction between two gluons), H_{sc} , and annihilation, H_{an} , of two gluons. Figure 1 depicts the three-gluon diagram for each interaction. The contribution from the self-energy term is

$$\frac{\langle \Psi | H_{\text{se}} | \Psi \rangle}{\langle \Psi | \Psi \rangle} = 18 \int d\mathbf{q}_1 d\mathbf{q}_2 d\mathbf{q}_3 F_{\mu_1\mu_2\mu_3}^* (\mathbf{q}_1, \mathbf{q}_2) F_{\nu_1\nu_2\nu_3} (\mathbf{q}_1, \mathbf{q}_2) \times D_{\mu_1\alpha}(\mathbf{q}_1) D_{\mu_2\nu_2}(\mathbf{q}_2) D_{\mu_3\nu_3}(\mathbf{q}_3) D_{\beta\nu_1}(\mathbf{q}_1) \times \left[\frac{\omega_1^2 + q_1^2}{2\omega_1} \delta_{\alpha\beta} - \frac{3}{4} \int \frac{d\mathbf{q}}{(2\pi)^3} \hat{V}(q) \times \frac{\omega_1^2 + \omega_6^2}{\omega_1\omega_6} D_{\alpha\beta}(\mathbf{q}_6) \right], \quad (8)$$

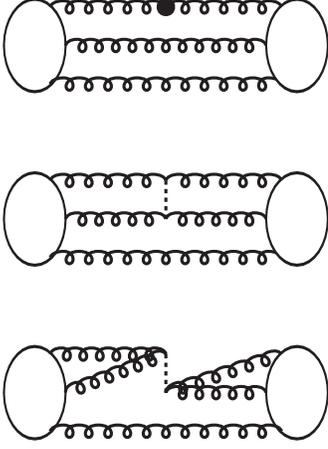


FIG. 1. Interaction diagrams for the ggg state in the H_{eff}^g approach. Top to bottom corresponds to the gluonic self-energy, scattering, and annihilation interactions, respectively.

where we have suppressed the J^{PC} superscript and the dependent variable $\mathbf{q}_3 = -\mathbf{q}_1 - \mathbf{q}_2$. Again $\omega_i = \omega(\mathbf{q}_i)$ is the solution to the gluon gap equation [4,20], $\mathbf{q}_6 = \mathbf{q}_1 + \mathbf{q}$, and \mathbf{q} is the momentum transferred by the interaction. Similarly the scattering contribution is

$$\begin{aligned} \frac{\langle \Psi | H_{\text{sc}} | \Psi \rangle}{\langle \Psi | \Psi \rangle} &= -\frac{9}{2} \mathcal{F}_{\text{sc}}^{\pm} \int d\mathbf{q}_1 d\mathbf{q}_2 d\mathbf{q} F_{\mu_1 \mu_2 \mu_3}^*(\mathbf{q}_1, \mathbf{q}_2) \hat{V}(q) \\ &\times F_{\nu_1 \nu_2 \nu_3}(\mathbf{q}_4, \mathbf{q}_5) \frac{(\omega_1 + \omega_4)(\omega_2 + \omega_5)}{\sqrt{\omega_1 \omega_2 \omega_4 \omega_5}} \\ &\times D_{\mu_3 \nu_3}(\mathbf{q}_3) D_{\mu_2 \beta}(\mathbf{q}_2) D_{\beta \nu_2}(\mathbf{q}_5) D_{\mu_1 \alpha}(\mathbf{q}_1) \\ &\times D_{\alpha \nu_1}(\mathbf{q}_4), \end{aligned} \quad (9)$$

with $\mathbf{q}_4 = \mathbf{q}_1 - \mathbf{q}$, $\mathbf{q}_5 = \mathbf{q}_2 + \mathbf{q}$. Finally the annihilation contribution is

$$\begin{aligned} \frac{\langle \Psi | H_{\text{an}} | \Psi \rangle}{\langle \Psi | \Psi \rangle} &= \frac{9}{4} \mathcal{F}_{\text{an}}^{\pm} \int d\mathbf{q}_1 d\mathbf{q}_2 d\mathbf{q} F_{\mu_1 \mu_2 \mu_3}^*(\mathbf{q}_1, \mathbf{q}_7) \hat{V}(q) \\ &\times F_{\nu_1 \nu_2 \nu_3}(\mathbf{q}_8, \mathbf{q}_2) \frac{(\omega_1 + \omega_7)(\omega_2 + \omega_8)}{\sqrt{\omega_1 \omega_2 \omega_7 \omega_8}} \\ &\times D_{\mu_3 \nu_3}(\mathbf{q}) D_{\mu_1 \alpha}(\mathbf{q}_1) D_{\mu_2 \alpha}(\mathbf{q}_7) D_{\nu_1 \beta}(\mathbf{q}_8) \\ &\times D_{\beta \nu_2}(\mathbf{q}_2), \end{aligned} \quad (10)$$

with $\mathbf{q}_7 = \mathbf{q} - \mathbf{q}_1$ and $\mathbf{q}_8 = \mathbf{q} - \mathbf{q}_2$. The first two contributions exactly cancel the infrared singularity in the instantaneous potential. The color factors $\mathcal{F}^{C=\pm}$ depend upon the C parity and follow directly from the expectation value of the density-density ($f^{abc} f^{aef}$) term in the Coulomb kernel: $\mathcal{F}_{\text{sc}}^+ = \frac{f^{abc} f^{aef} f^{bei} f^{cfi}}{f^{abc} f^{abc}} = \frac{-36}{24} = -\frac{3}{2}$, $\mathcal{F}_{\text{sc}}^- = \frac{d^{abc} d^{aef} f^{bei} f^{cfi}}{d^{abc} d^{abc}} = \frac{-20}{40/3} = -\frac{3}{2}$, $\mathcal{F}_{\text{an}}^+ = \frac{f^{abc} f^{aef} f^{bei} f^{cfi}}{f^{abc} f^{abc}} = \frac{72}{24} = 3$, and $\mathcal{F}_{\text{an}}^- = \frac{d^{abc} d^{aef} f^{bei} f^{cfi}}{d^{abc} d^{abc}} = \frac{0}{40/3} = 0$, using the orthogonality relation $d^{abc} f^{abc} = 0$ and computer algebra [FORM [24]]. The H_{an} interaction splits the 0^{-+} s wave glueball state from the 1^{--} and 3^{--} levels, all calculated degenerate in the work of Ref. [14]. Also, annihilation is not

present in simple ggg potential models as well as all models for gg states which is why it has not been studied previously in investigations of the lightest 0^{-+} mass, involving p wave two-gluon states, calculated between 2.1 GeV [16] and 2.6 GeV [25].

The variational calculation entails nine-dimensional integrals which were performed using the Monte Carlo method with the adaptive sampling algorithm VEGAS [26]. In general, numerical convergence was achieved with about 10^5 samples. A study of the glueball mass sensitivity to both statistical and variational uncertainties yielded error bars at the 3 to 5% level.

For comparison we also calculated oddball masses using a simpler nonrelativistic constituent model Hamiltonian [27]

$$H_M = \sum_i \frac{\mathbf{q}_i^2}{2m_g} + V_0 + \sum_{i < j} \left[\sigma r_{ij} - \frac{\alpha}{r_{ij}} + V_{\text{ss}} \mathbf{S}_i \cdot \mathbf{S}_j \right], \quad (11)$$

with $r_{ij} = |\mathbf{r}_i - \mathbf{r}_j|$ and parameters taken from the $q\bar{q}$ funnel potential: $V_0 = -0.90$ GeV, $\alpha = 0.27$, $\sigma = 0.25$ GeV². The gap equation gluon mass value, $m_g = 0.8$ GeV, is also used. Exactly diagonalizing, $H_M \Psi^{\text{JPC}} = M_{\text{JPC}} \Psi^{\text{JPC}}$, and only adjusting $V_{\text{ss}} = 0.085$ GeV to optimize agreement with lattice, yields the predicted J^{++} glueball Regge trajectory, $\alpha_P^M = 0.23t + 1.0$, consistent with the Pomeron. In the gg glueball calculation an algebraic color factor of 2 multiplies each bracketed term in the potential. With these fixed parameters the ggg oddball spectrum was then obtained by exact diagonalization using Jacobi coordinates and an expansion in a harmonic oscillator basis. Further details will be reported in a future communication.

The glueball masses and quantum numbers investigated are listed in Table I. Note that the H_{eff}^g ground state for the ggg glueball is technically not an oddball but the 0^{-+} with mass 3900 MeV. Also, the model ggg glueballs are heavier than gg states (both having low excitations) which is consistent with predictions deduced from the holographic

TABLE I. Glueball quantum numbers and masses in MeV. The errors in our H_{eff}^g (from Monte Carlo calculations only) are 100 MeV or less; the quoted lattice errors are typically 200–300 MeV. Within these bounds the agreement is encouraging. Notice our calculation is adjusted independently to the lattice 0^{++} .

Model	J^{PC}	0^{-+}	1^{--}	2^{--}	3^{--}	5^{--}	7^{--}
	color	f	d	d	d	d	d
	S	0	1	2	3	3	3
	L	0	0	0	0	2	4
H_{eff}^g (this work)		3900	3950	4150	4150	5050	5900
H_M (this work)		3400	3490	3660	3920	5150	6140
Lattice [25]		3640	3850	3930	4130		
Lattice [5]		3250	3100	3550	4150		
Wilson loops [28]		3770	3490	3710	4030		

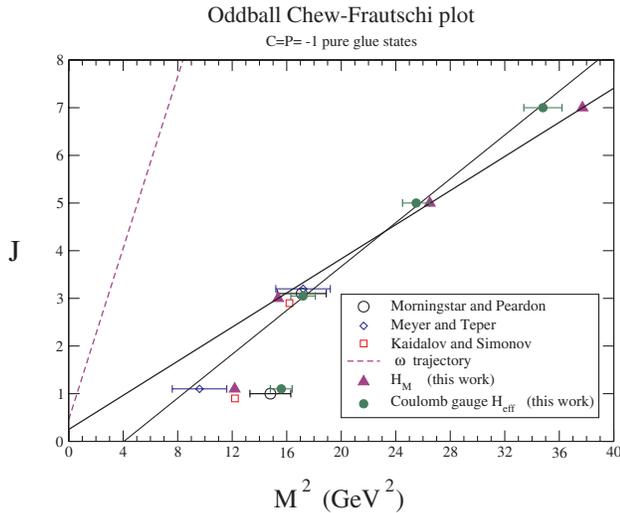


FIG. 2 (color online). Odderon trajectory from three-gluon spectroscopy and lattice compared to the ω meson Regge trajectory.

dual theory of QCD [29]. Figure 2 summarizes our key findings and displays predicted oddball Regge trajectories from the alternative approaches. Lattice results are represented by diamonds [5] and open circles [25], while boxes [28] are constituent model predictions using a Wilson-loop inspired potential. Solid circles and triangles correspond to the H_{eff}^g and H_M models, respectively. The resulting odderon trajectories are represented by the solid lines, $\alpha_O^{\text{eff}} = 0.23t - 0.88$ and $\alpha_O^M = 0.18t + 0.25$, whose differences provide an overall theoretical uncertainty. The dashed line is the ω trajectory.

Several conclusions follow. First, this work predicts an odderon having slope similar to the Pomeron but intercept even lower than the ω value. Second, the first odderon state is the 3^{--} and not the 1^{--} which falls on a daughter trajectory. Unfortunately, the other approaches did not report a 5^{--} glueball which could confirm this point. Since at least two points are necessary to establish a trajectory we strongly recommend that future studies calculate higher J states. Lastly, there appears to be general model consensus that the 3^{--} mass is close to 4 GeV and also support for the 0^{-+} as a ground state candidate for the ggg system.

In summary, we have compared existing oddball predictions to our large-scale model evaluations for J^{--} glueballs. The results document an odderon trajectory subdominant to the Pomeron which can explain its non-observance in reactions with Pomeron exchange. Should the odderon intercept be comparable to the ω value it may be possible to see it in pseudoscalar [30] or tensor meson [31] electromagnetic production where the Pomeron is absent. However, if the intercept is below 0.5, as we predict, it is unlikely the odderon will be observed.

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